

Speed limit to the Abrikosov lattice in mesoscopic superconductorsG. Grimaldi,^{1,*} A. Leo,^{1,2} P. Sabatino,^{1,2} G. Carapella,^{1,2} A. Nigro,^{1,2} S. Pace,^{1,2} V. V. Moshchalkov,³ and A. V. Silhanek⁴¹*CNR SPIN Salerno, via Giovanni Paolo II, 132, 84084 Fisciano (SA), Italy*²*Physics Department “E. R. Caianiello,” University of Salerno, 84084 Fisciano (SA), Italy*³*INPAC and Nanoscale Superconductivity and Magnetism Group, K. U. Leuven, Celestijnenlaan 200D, B-3001 Leuven, Belgium*⁴*Département de Physique, Université de Liège, B-4000 Sart Tilman, Belgium*

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We study the instability of the superconducting state in a mesoscopic geometry for the low pinning material Mo₃Ge characterized by a large Ginzburg-Landau parameter. We observe that in the current-driven switching to the normal state from a nonlinear region of the Abrikosov flux flow, the mean critical vortex velocity reaches a limiting maximum velocity as a function of the applied magnetic field. Based on time-dependent Ginzburg-Landau simulations, we argue that the observed behavior is due to the high-velocity vortex dynamics confined on a mesoscopic scale. We build up a general phase diagram which includes all possible dynamic configurations of the Abrikosov lattice in a mesoscopic superconductor.

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I. INTRODUCTION

Continuous advancements in nanofabrication have permitted exploration and discovery of new emergent physical phenomena when approaching the meso- and nanoscopic limit [1–4]. The stability of the superconducting state under geometrical confinement is now intensively investigated due in part to the anomalous mixed state in type-II superconductors [5,6], as well as for reaching a better performance in their potential applications [7]. Unfortunately, one rarely witnesses the persistence of the nondissipative regime up to the depairing current density J_{dp} due to the current-induced motion of magnetic flux quantum units (Abrikosov vortices) and the consequent Joule heating for currents above a critical current $J_c < J_{dp}$. The actual discrepancy between the theoretical expectation and the experimental fact has its origin in the largely neglected nonequilibrium phenomena occurring at the core of the swiftly moving Abrikosov vortices [8,9]. One of these effects, taking place at intermediate current densities $J_c < J^* < J_{dp}$, consists of a deformation of the flux quanta core due to the slow healing time of the superconducting condensate after the passage of a vortex singularity in the condensate [10]. As a consequence, a rapidly moving vortex leaves behind a trail of depleted order parameters that further facilitates the motion of other vortices, thus forming rivers of flux leading to a net increase of dissipation and triggering an abrupt transition from the Abrikosov flux flow regime to the normal state [11,12]. No matter which mechanism is responsible for this current instability [10–15], in this work we show that in the mesoscopic regime, the average critical velocity needed to trigger the instabilities is limited by a maximum speed value that is not observed under no confinement. We investigate the so far unexplored mesoscopic regime where the scenario based on pinning disorder is of no application due to the fact that we use an extremely weak pinning superconducting material, Mo₃Ge, in which free flux flow has been recently confirmed [16]. Many studies have been carried out in order to address other possible competing effects,

such as the influence of pinning properties of the intrinsic material [17,18] and the artificially structured superconductors [19]. Nevertheless, in all these cases the geometry of the test sample has been kept on a macroscopic scale. Here we demonstrate that the Abrikosov lattice instability is affected by a significant surface barrier in mesoscopic superconductors. Time-dependent Ginzburg-Landau simulations satisfactorily reproduce the experimental results and give a complete overall description of Abrikosov vortex dynamics driven at high velocity. This can be a general example for high-velocity dynamics in any context of confined geometry, for example, in the dynamics of magnetic entities such as Skyrmions [20], in flows and mixing in microfluidic devices [21], as well as in the high-speed impact of fluid within a granular material [22].

II. EXPERIMENTAL RESULTS**A. Vortex pinning properties**

Mo₃Ge thin films were grown on Si/SiO₂ substrates by pulsed laser deposition technique using a Nd:YAG ($\lambda = 532$ nm) pulsed laser of 55-J energy and a repetition rate of 10 Hz. The deposition was performed at a pressure of 10^{-7} mbar. Using these parameters, a deposition rate of 1.1 nm/min is achieved. All depositions were done on Si wafers with an amorphous SiO_x top layer. Microbridges were obtained by electron-beam lithography with thickness $d = 50$ nm, length $L = 160$ μ m, and different linewidths $w = 5 \div 100$ μ m [23].

The superconducting properties strongly depend on the thickness of the films. For 4-nm-thick films, there is no superconducting transition. For films thicker than 25 nm, the superconducting transition saturates, reaching values up to 7 K [23]. Typical values of the superconducting parameters for the highest T_c film, namely, S100, are $T_c = 6.5$ K, $H_{c2}(0) \sim 9$ T, $J_c(0) = 0.15$ MA/cm². In addition, it has been shown that usually the irreversible magnetization loops are already closed at 20 mT, i.e., 2 orders of magnitude smaller than H_{c2} [24].

Pulsed current-voltage (I - V) measurements were performed in order to minimize self-heating effects [17]. Since unavoidable self-heating may affect experimental data, first

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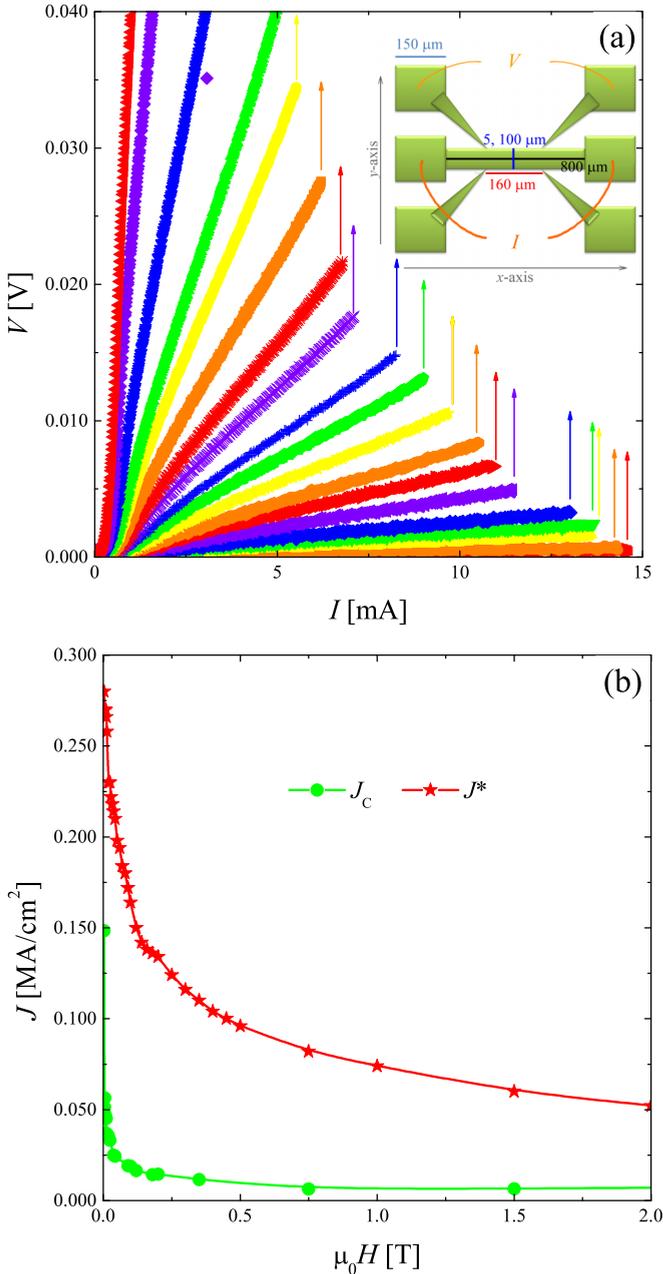


FIG. 1. (Color online) (a) The I - V curves for the 100- μm -wide strip S100 at $T = 1.6$ K and $H = 0.9, 2.5, 6.0, 9.5, 13, 24, 33, 43, 60, 81, 100, 140, 180, 250, 350, 451, 750, 1497,$ and 2494 mT. In the inset the sample layout is sketched. (b) Critical and instability current densities as a function of the applied magnetic field extracted from the I - V curves.

of all we chose a pulsed biasing mode with a pulse width of 2.5 ms and an inter pulse period of 1 s [25].

In Fig. 1 the I - V curves for the measured S100 macroscopic strip are shown along with the data related to the critical current density J_c and the instability current J^* as a function of the applied magnetic field. We note that for the whole field range, J_c is considerably smaller than J^* and exhibits a very steep decrease as a function of the magnetic field. The absolute J_c values of the order of 10^4 A/cm² reveal the weak pinning nature of this material.

B. Vortex lattice instability at the mesoscopic scale

The mesoscopic limit is reached when $d \ll \lambda$ [26–28], with λ the London penetration depth, and the sample width is narrower than the Pearl length $w \leq \Lambda = 2\lambda^2/d$ [26] and much wider than the Ginzburg-Landau coherence length $w \gg \xi_{GL}$. The estimated values of effective coherence length and penetration depth at very low temperatures for our Mo₃Ge films are as low as $\xi_{GL} \simeq 5$ nm and as large as $\lambda = 500$ nm, corresponding to a large Ginzburg-Landau parameter $k = 100$. The conditions for the mesoscopic limit are reasonably satisfied for our thin films of $w = 5$ μm being $\Lambda = 10$ μm . On these mesoscopic samples we checked that self-heating effects can be neglected. Indeed, no hysteresis occurs in the I - V curves by performing measurements forth and back (increasing and subsequently decreasing current) of each curve by current biasing. Moreover, we can assure that the instability point of each curve remains unchanged and it is always reproducible, although at low fields the metastable states can change before the normal state is reached. We also took into account self-heating by considering the Bezuglyi-Shklovskij approach for the term of quasiparticle overheating [13], leading to the estimate of the threshold magnetic field value $B_T = 0.374eh\tau_E/k_B\sigma_N d \sim 3$ T, where h is the heat-transfer coefficient to the coolant [29], τ_E is the quasiparticle relaxation time [16], and σ_N is the normal conductivity [23]. In other words, heating effects become significant for $B > B_T$, out of the field range in which the maximum speed limit of the moving Abrikosov lattice is achieved. In addition, we derived from the I - V data of Fig. 1(a) the dissipated power $P^* = I^*V^*$, which is an increasing function of the magnetic field, as shown in Fig. 2. This is the experimental evidence that thermal effects are not determining the flux flow instability points. Indeed, if this was the case of a thermal runaway, P^* should be independent of magnetic field, as already pointed

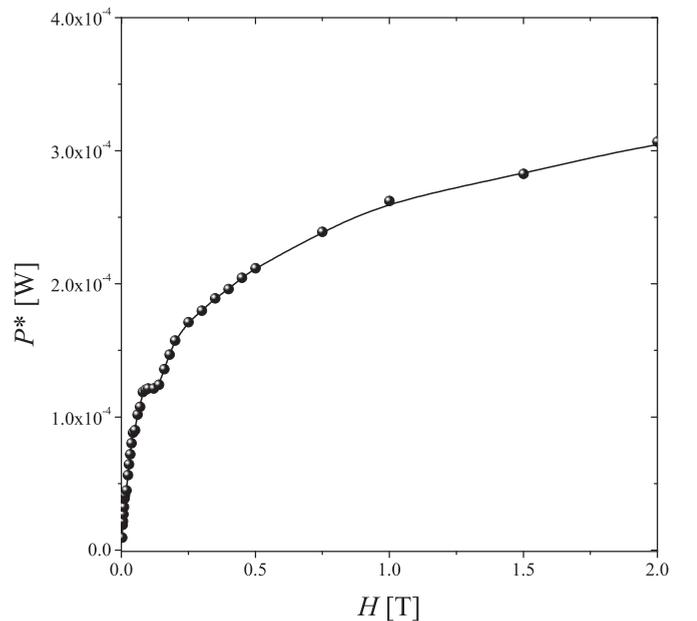


FIG. 2. The dissipated power as a function of the magnetic field. Each data is estimated at the instability points marked by the arrows in Fig. 1(a).

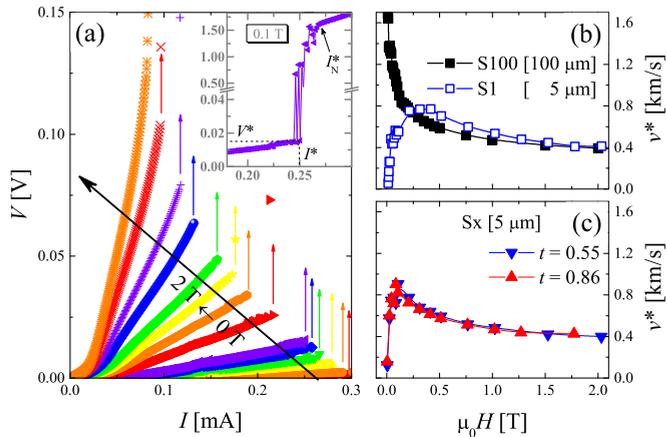


FIG. 3. (Color online) (a) Experimental I - V curves at $T = 1.6$ K for increasing magnetic field (as indicated by the arrow, in mT): 4, 25, 46, 67, 87, 109, 209, 311, 412, 513, 767, 1023, 1526, and 2031. The inset shows several multiple jumps before reaching the normal resistance. (b) The critical vortex velocity as a function of magnetic field for the S100 and S1 strips, indicated by the full and open symbols, respectively. (c) The $v^*(\mu_0 H)$ curves for two reduced temperatures $t = 0.55$ and 0.86 measured on the Sx strip. Lines are guide to the eye.

out by Xiao *et al.* [30]. We also note that this magnetic field dependence has been predicted by Vina *et al.* [31] on self-heating-based calculations. However, they deal with a high-temperature superconductor, yttrium barium copper oxide (YBCO) microbridges, in a temperature range close to T_c , $0.8 < T/T_c < 1$, whose normal-state resistivity are several orders of magnitude larger than in our mesoscopic strips.

In Fig. 3(a) we report the I - V curves as a function of magnetic field for the 5- μm mesoscopic strip Sx at the lowest temperature $T = 1.6$ K. The inset shows a single curve measured at low field in which multiple voltage jumps are observed in the $V(I)$ branch above the instability point (I^*, V^*) and up to the normal current I_N^* . In this case, the transition to the normal state follows several metastable states, instead of being an abrupt voltage jump.

Mo₃Ge being considered a weak pinning superconductor, almost linear flux flow branches are also expected up to high bias current, as it is noticed both for Sx [see Fig. 3(a)] and the 100- μm strip S100 [see Fig. 1(a)]. From the last point (I^*, V^*) marked by the arrows in the continuous branch, we estimate the mean critical velocity of the moving vortex lattice as $v^* = E^*/\mu_0 H$. By extracting the $v^*(\mu_0 H)$, we obtain a surprising result: the size reduction down to the mesoscopic scale implies the change of the critical velocity behavior in a substantial magnetic field range $\mu_0 H < 0.5$ T, as shown in Fig. 3(b) for the case of the 5- μm mesoscopic strip S1 and the S100 macroscopic one. Interestingly, from the fact that v^* estimations acquired at two different temperatures [see Fig. 3(c)] show no difference, we can suggest that the observed change in v^* for the mesoscopic sample is rather T independent.

C. Pinning effect on vortex instability

In order to investigate if the observed behavior $v^*(\mu_0 H)$ in the mesoscopic limit is influenced by any bulk pinning, we

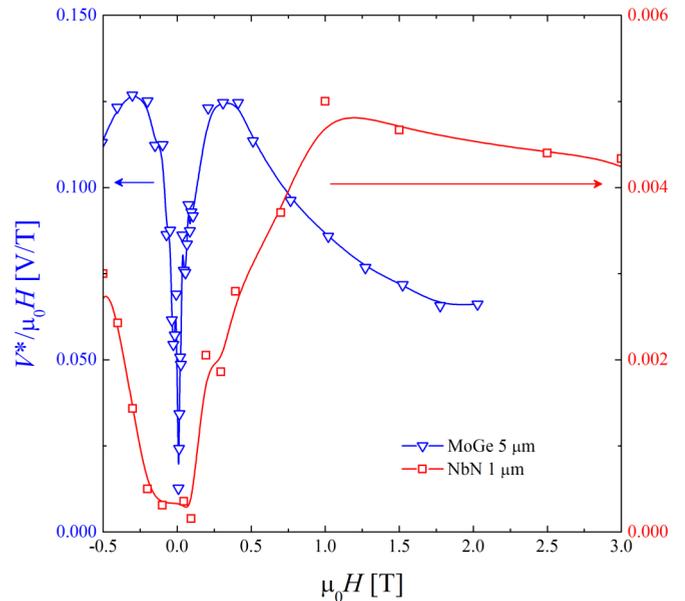


FIG. 4. (Color online) Critical voltages vs magnetic field. Data acquired on a mesoscopic NbN stronger pinning superconducting strip (squares) compared with the Mo₃Ge S1 mesoscopic strip (triangles).

changed the intrinsic pinning from the weak Mo₃Ge thin films to a well-known, stronger pinning superconductor, namely, NbN.

We fabricated a mesoscopic strip of 1 μm width and 10 μm length, realized by e-beam lithography on $d = 20$ -nm thin film, so that we obtained $\lambda(0) = 400$ nm and $\Lambda = 16$ μm . By carrying out the same data analysis performed in the case of the Mo₃Ge samples, we obtained the results collected in Fig. 4, where the critical voltages of the NbN sample are plotted together with the data related to the Mo₃Ge sample S1. We find that even a strong pinning material on the mesoscopic scale has the same striking behavior, although on a larger magnetic field range.

III. NUMERICAL SIMULATIONS

A. Model

Time-dependent Ginzburg-Landau (TDGL) simulations are used to gain information on the vortex dynamics accounting for the I - V curves observed in the Mo₃Ge mesoscopic superconductor. We use the TDGL model in its two-dimensional (2D) simplified form, being justified when the strip exhibits a large parameter k and it is in the mesoscopic limit, which is our experimental case. In the mesoscopic limit current density is reasonably uniform and the magnetic field induced by the transport and screening currents can be usually neglected [26–28]. Moreover, in the model we neglect intrinsic bulk pinning, according to experimental data.

In the numerical simulations we assume the strip width to be equal to $w = 160\xi_L$ in the x direction and length $L = 80\xi_L$ in the y direction. Experimentally, the phenomenon we want to describe is found almost independent of temperature, $v^*(\mu_0 H, T)$, and it is recorded up to the reduced temperature $t = 0.86$. At this reduced temperature the normalized width of

the real strips is $w = 370\xi_L$. Indeed, we use the smaller width $w = 160\xi_L$ in the simulations as well, because we checked that the vortex dynamics involved did not change appreciably if such dimensions were further increased and because it would be more cumbersome to present snapshots of vortex dynamics covering the larger width of $370\xi_L$, the vortex cores being extended for only about $3\xi_L$.

We also underscore that in the nonmesoscopic regime with no bulk pinning (see, e.g., Ref. [11]) the current distribution is strongly peaked at edges of the strip and the current-assisted vortex nucleation is present also at fields $H < H_S/2$, where H_S is the field at which static vortices are present in the strip also for $J = 0$ [27,28,32]. In particular, at zero applied field the vortices and antivortices nucleate at the edges and annihilate at the center of the strip [11]. On the contrary, the region $0 < H < H_S/2$ of hampered vortex nucleation is observed in a mesoscopic system, compelling a vortex velocity increase with magnetic field from zero to a maximum value. This region can be hidden in the macroscopic system, where the finite (maximum) value of the average velocity can be achieved already at very low fields close to $H = 0$. This may account for the different behavior of $v^*(\mu_0 H)$ in the mesoscopic strip with respect to the macroscopic case.

In the following we assume that to work in a temperature range so close to T_c , the phenomenological TDGL model is supposedly adequate. The 2D TDGL equation for the complex order parameter $\psi = |\psi|e^{i\phi}$ takes the form [28,33,34]

$$u \left(\frac{\partial}{\partial t} + i\phi \right) \psi = (\nabla - i\mathbf{A})^2 \psi + (1 - |\psi|^2) \psi, \quad (1)$$

coupled with the equation for the electrostatic potential $\nabla^2 \phi = \text{div}\{\text{Im}[\psi^*(\nabla - i\mathbf{A})\psi]\}$, where \mathbf{A} is the vector potential associated to the external magnetic field H , ϕ is the electrostatic potential, and the coefficient $u = 5.79$ governs the relaxation of the order parameter [35]. All physical quantities are measured in dimensionless units [28,33,34]: the coordinates are in units of the coherence length $\xi_{GL}(T)$, time is in units of the relaxation time τ , the order parameter is in units of the superconducting gap $\Delta(T)$, the vector potential is in units of $\Phi_0/2\pi\xi_{GL}$ (where Φ_0 is the quantum of magnetic flux), and the electrostatic potential is in units of $\phi_0(T) = \hbar/2e\tau$. In these units the magnetic field is scaled with $H_{c2}(T) = \Phi_0/2\pi\xi_{GL}^2$ and the current density with $j_0(T) = c\Phi_0/8\pi^2\lambda^2\xi_{GL}$. The field H is applied in the z direction and the current density J is applied in the y direction. We make use of the ‘‘bridge’’ boundary condition in the y direction and of an insulator-superconductor boundary condition in the x direction [28,33,34].

B. Flux flow results

In Fig. 5(a), we show the calculated $E(J)$ curves, in the low-electric-field-range, for several values of magnetic field H applied perpendicular to the strip. Curves display a fully linear (at moderate and high fields) or nearly linear (at low fields) flux-flow branch starting at some critical current J_c in the rather large current range $J_c < J < J_l^*$, followed by a deviation from linear behavior in the limited current range $J_l^* < J < J^*$ and ending with a more or less abrupt transition to the fully normal state. The red line is displayed as a guide to the eye to mark the critical points (E_l^*, J_l^*) where the departure

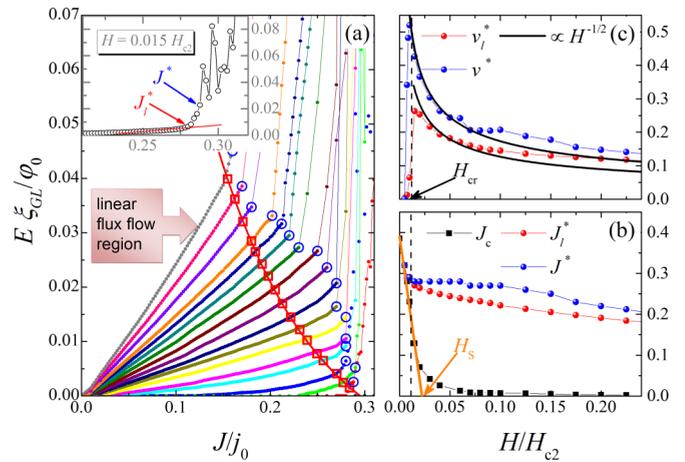


FIG. 5. (Color online) Numerical results: (a) $E(J)$ curves for different magnetic field values in the low-electric-field range. In units of H_{c2} the field values are 0.0075 (red dots), 0.01, 0.015, 0.03, 0.04, 0.06, 0.08, 0.1, 0.125, 0.15, 0.175, 0.2, 0.225, 0.25, 0.3, 0.35, and 0.4 (gray dots). The inset shows a single curve at low field. (b) Critical and instability current densities as a function of magnetic field. (c) Average vortex critical velocities for the linear and nonlinear regimes as a function of magnetic field.

from almost linear behavior occurs. The circles mark the instability points (E^*, J^*) at which the continuous nonlinear branch ends and a very high differential resistivity branch (at moderate/high fields) or a metastable branch (at low fields) is followed before transition to the normal state is achieved. Figure 5(b) shows the relevant current densities J_l^* , J^* , J_c as a function of magnetic field. The average critical velocity of the linear $v_l^* = E_l^*/\mu_0 H$ and nonlinear $v^* = E^*/\mu_0 H$ regimes are plotted as a function of applied magnetic field in Fig. 5(c). In analogy with experimental data, both critical velocities exhibit a nonmonotonic behavior with a maximum at a certain field H_{cr} , after which a decreasing function of H is established, approximately, as $H^{-1/2}$ [17]. In the following we focus on the vortex dynamics accounting for the $E(J)$ in the magnetic field range around H_{cr} where such a crossover is found [see Fig. 5(c)] and v_{max}^* is reached. In Fig. 5(b) we can distinguish, in the magnetic field range in which the critical velocity is increasing, the ‘‘entry field’’ $H = H_S$, that is $H_S = 0.021 H_{c2}$. Inspection of Figs. 5(b) and 5(c) suggests that the crossover field H_{cr} can essentially be identified with $H_S/2$.

C. Nonequilibrium phase diagram

At magnetic fields larger than the entry field H_S , a regular Abrikosov vortex lattice is expected to be present even at $J = 0$. At fields $H_S/2 < H < H_S$, by increasing the driving current, vortices nucleate to the left edge of the strip but start to flow only at some finite current J_c due to the presence of a surface barrier in the system [27,28]. Though a triangular vortex lattice is not fully created, there exists a quasiordered motion of vortices (see snapshot I in Fig. 6) that results in an almost linear branch in the $E(J)$ curve up to J_l^* . By further increasing current, a departure from the nearly linear $E(J)$ curve occurs up to the critical current J^* , and vortex flow transforms to a rowlike structure, as visualized in snapshot

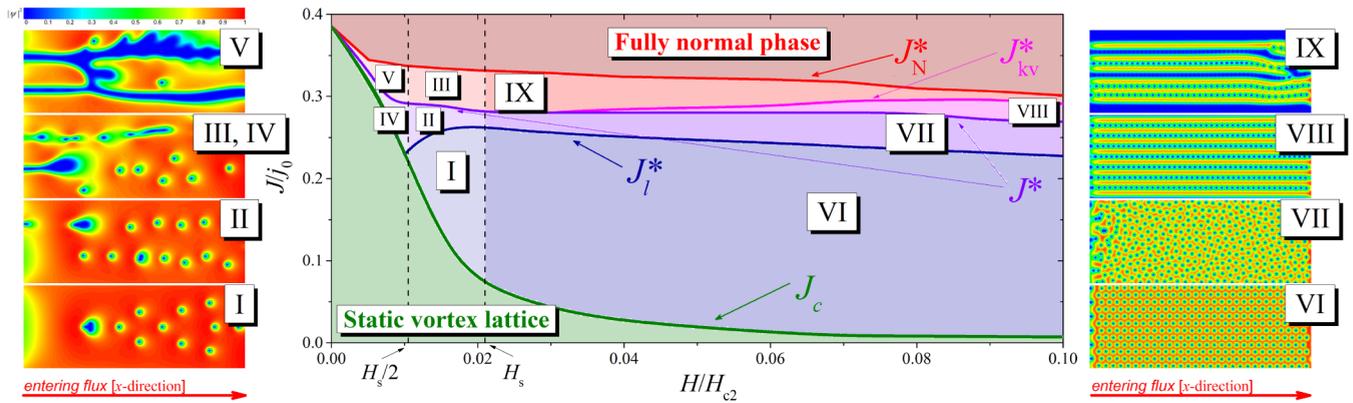


FIG. 6. (Color online) Numerically obtained dynamic phase diagram of vortex lattice in a mesoscopic superconductor. It is identified by the peculiar entry field $H = H_S$ above which a regular vortex lattice can be set in motion, as well as the instability current density J^* above which moving ordinary vortices transform in kinematic vortices at moderate or high fields or ordinary vortex bundles mixed to clustered normal regions at low field. When present, normal regions expand at the expense of vortex matter with increasing current up to a final J_N^* where the system undergoes the transition to the fully normal state. Snapshots show the evolution of the vortex lattice configuration upon increasing the driving current.

II. At currents larger than J^* the row structure evolves into a normal channel-like configuration, as shown in snapshot III. This corresponds to a noisy behavior in the $E(J)$ curve and to dynamical states in which the presence of vortices is restored at the expense of normal channels [see inset of Fig. 5(a)]. For fields $H < H_S/2$, we note only the sequence of states, which in our analysis involves the transition to the normal state with a more or less pronounced intermittent effect (see snapshots IV and V). Interestingly, this intermittence is also observed in the experimental curves [see inset of Fig. 3(a)]. We should remark that, for the magnetic field range $H_S/2 < H < H_S$, there exists a finite current range where nearly ordered vortex matter is driven by the bias current. In this lower field region vortices can nucleate in the strip only when a quite large uniformly distributed transport current ($\sim J_{dp}$) helps the screening current to suppress the order parameter at one of the edges of the strip, thus promoting vortex nucleation [28,32,36].

In Fig. 6 we include the full zoology of vortex lattice phases in motion, with particular attention on the dynamic phase diagram in which nonlinearity arises. Here some well-known phases are reported for completeness: the static vortex lattice which exists only for $J < J_c$, and the fully normal phase for $J > J_N^*$. In the low-field region $H_S/2 < H < H_S$, region I corresponds to the current-assisted vortex nucleation with an almost triangular moving vortex lattice, which results in the almost linear flux flow motion $J_c < J < J_l^*$. At larger currents we find other two possible nonequilibrium phases, II and III. In Region II ($J_l^* < J < J^*$), a rowlike moving vortex lattice can exist with a corresponding filamentary displacement of vortices (vortex river). For larger currents clusters of normal metal phase develop which match the intermittence phase III with metastable states before reaching the fully normal phase. In agreement with analytical predictions presented in Ref. [32], in the field range $0 < H < H_S/2$, transport-current-assisted discrete vortex nucleation is practically absent. Here, we only observe a disordered bundlelike vortex nucleation and motion, accounting for a strongly nonlinear $E(J)$ branch up to J^* (region IV), followed by a regime (region V) where flux bundles are mixed to a clustered normal phase, as shown in

snapshot V of Fig. 6. At $H > H_S$, region VI corresponds to the ordinary linear flux flow accounted for by a moving triangular lattice (snapshot VI). This regular motion is observed up to a critical current J_l^* , resulting in a nearly linear branch of the $E(J)$ curve. Region VII marks the nonlinear flux flow motion for $J_l^* < J < J^*$, accounted for by a moving glassy lattice (snapshot VII). Above the instability current J^* , jumps to high resistivity branches can occur (region VIII). These branches, which extend in the range $J^* < J < J_{kv}^*$, are accounted for by a channel-like structure of vortices, as shown in snapshot VIII, very similar that described in Ref. [11]. For $J > J_{kv}^*$, the vortex channel structure leads to the opening of normal channels (see snapshot IX), which are responsible for a more or less abrupt transition to the highest resistive state, i.e., the normal state. Fast (kinematics) vortices surfing on channels of very depressed superconductivity shown in snapshot VIII were investigated in detail in Ref. [11] within the generalized TDGL model that accounts for the nonequilibrium effects through a parameter γ [35]. In our simulations we used the standard TDGL with $\gamma = 0$ and, though present, the high-resistivity branches accounting for kinematic vortices are consistently [35] recovered only in a current range much narrower than that found in Ref. [11].

IV. CONCLUSIONS

In the framework of vortex dynamics we identify the limiting behavior of the Abrikosov lattice stability driven at high vortex velocity in the absence of bulk pinning, with the only constraint being confined mesoscopic geometry. The possibility to reach a maximum critical velocity as a function of the applied magnetic field is naturally explained by the TDGL phenomenological approach, which allows us to give a complete view of nonequilibrium vortex phases tunable by the external magnetic field and/or the bias current in a dynamic phase diagram. In a mesoscopic superconductor the physical meaning of such a speed limit to the Abrikosov vortex velocity is strictly connected to the presence of surface pinning, namely, an edge barrier, which first hampers and then delays the lattice

motion, due to the rearrangement of vortice configuration in rowlike flow rather than keeping the usual ordered triangular vortex lattice in motion. To visualize it, real-space images of the driven lattice show that motion occurs along channels that are aligned with the direction of the driving force and periodically spaced in the transverse direction. Phase slips, however, occur at the channel boundaries, indicating that channels become uncorrelated at very high driving current, before the instability takes place. In our case those channels may exist only at a velocity $v < v^*(H_{cr}) = v_{\max}^*$, which is the speed limit for the moving Abrikosov lattice.

The sequence in which these dynamical phases appear at high bias currents is usually nontrivial, and the simplified models of vortices as pointlike classical particles seem to have missed what a more realistic approach based on TDGL formalism is able to catch [37].

A further comparison of data on weak Mo₃Ge superconductors with the bulk pinning effects in NbN surprisingly led to

similar results, thus conferring to our findings even more generality. Our results demonstrate that geometric reduction on a mesoscopic scale can radically change the dissipative regimes in superconducting materials, thus improving the performance of those devices based on superconducting nanostructures.

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