

Reinforced concrete beams strengthened with SRP/SRG systems: Experimental investigation

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REINFORCED CONCRETE BEAMS STRENGTHENED WITH SRP/SRG SYSTEMS: EXPERIMENTAL INVESTIGATION

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ABSTRACT

Steel reinforced polymer (SRP) and steel reinforced grout (SRG) have emerged as promising and cost-effective technologies for the external strengthening of RC structures.

Although the first studies date back to 2004, so far the literature related to the flexural strengthening of RC slab/beams with steel tapes is rather limited. As a result, the application of such materials on a real structural member may be discouraged and, conversely, the use of carbon/glass FRP alternative systems may be preferred.

The study presented in this paper contributes to filling this knowledge gap by presenting the results of 10 four-point bending tests performed on RC slabs strengthened with SRG/SRP systems. Test results have provided valuable information in terms of maximum forces, deformability and failure modes by varying number of layers and density of the steel tape. In particular, it has been shown that, disregarding the nature of the matrix (inorganic or polymeric), the presence of the external strengthening significantly increased the flexural strength of slabs, with percentage increases over the control (unstrengthened) member ranging from a minimum value of 27%, when using a single layer of low density tape, to a maximum of 106% in the case of SRP system with one layer of high density sheet.

Preliminary analytical studies were also performed in order to investigate the possibility of extending to the SRP/SRG systems the applicability of formulations currently reported in some national and international guidelines for the flexural strengthening of RC members with FRP sheets.

Keywords: Epoxy; Experimental tests; Flexural strengthening, Grout; Steel tapes; Strain; Strength.

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34 **1. Introduction**

35 Over the years, the use of Fiber Reinforced Polymer (FRP) materials for the strengthening of reinforced
36 concrete (RC) structural members has met an increasingly widespread consensus at both the academic
37 and industrial levels, representing today a competitive alternative to traditional techniques.

38 In the case of external strengthening, it is well known that behind the FRP terminology, systems
39 employing carbon fibers are typically referred to, whereas fewer applications make use of glass or aramid
40 fibers. The successful application of such composites in the civil engineering has also been recognized
41 through the spread of specific guidelines around the world, such as the Italian Guidelines CNR-DT 200
42 R1 [1] and the American Guidelines ACI 440.2R [2].

43 However, the growing interest in the composites industry towards the development of innovative and low
44 cost solutions has led to the introduction of new techniques for the structural reinforcement that make use
45 of other fibers in lieu of the carbon or glass ones. Among the “new generation” materials, the class of
46 composites made of steel fiber sheets has emerged as one of the most promising and cost-effective
47 solutions for external strengthening of RC members.

48 The steel tape consists of high carbon steel cords made by twisting steel wires within a micro-fine brass
49 or galvanized coating; it can be in situ applied via wet lay-up by using epoxy resin or inorganic matrix,
50 thus obtaining strengthening systems known with the acronym of SRP (“*Steel Reinforced Polymer*”) and
51 SRG (“*Steel Reinforced Grout*”), respectively. The tape can be required according to different densities
52 (generally denoted as low, medium or high), depending on the number of wires distributed in the sheet
53 width.

54 Although the first studies date back to 2004 [3,4], so far the scientific papers dealing with the use of steel
55 fiber composites for the strengthening of RC structural members (due to bending, shear, or confinement
56 deficiencies) are rather limited, as well as specific guidelines have not been published yet. As a result, the
57 lack of an extensive knowledge on the applicability of these materials might guide the designer toward
58 the choice of “proven” strengthening solutions or more marketed composite systems, i.e., those
59 employing the above mentioned carbon or glass fibers.

60 By focusing on the flexural strengthening of RC beams/slabs with steel fiber materials, the bibliography
61 reports the main papers by authors contributing to provide some information about the effectiveness of
62 using SRP/SRG systems in the structural rehabilitation [3-15]. In particular, the experimental studies

63 performed by Wobbe et al. [3], by Prota et al. [5], by Kim et al. [6] and Balsamo et al. [9], are pointed out.
64 Wobbe et al. [3] just performed a first experimental study devoted to prove the potential of the SRP/SRG
65 technology in improving the performance of RC members.

66 In addition to highlight the influence of using different tape densities on the specimens' response, Prota et
67 al. also investigated the flexural behaviour of beams strengthened with SRG sheets mechanically
68 anchored to the concrete substrate by using nail anchors. It was shown that such nails do not improve the
69 performance of the steel tape impregnated with cementitious grout, being the used tape of unidirectional
70 type, as generally commercialized in the market; in fact, lacking a transverse link, the distribution of the
71 local stress concentration at anchor location was not allowed; as a result, the subsequent bearing failure of
72 nails was unable to improve the bond and delay the tape debonding [5].

73 Kim et al., instead, examined the efficiency of the SRP system by varying the width of the employed tape
74 and the beneficial role played by the use of U-shape SRP wraps as end anchorages to prevent the peeling-
75 off failure of the external reinforcement at the beam's intrados [6]. It was again proven the positive
76 contribution of the SRP reinforcement in increasing the flexural capacity of RC beams; also, it was shown
77 that the U-wraps improve the flexural stiffness by controlling diagonal crack width and providing
78 anchorages to the longitudinal SRP sheets, which reduces their slip.

79 Finally, a comparative analysis of different composite material systems (CFRP-SRP-SRG) for the flexural
80 strengthening of prestressed RC beams was performed by Balsamo et al. [9]; in that work, the
81 convenience into using steel fiber sheet with respect to the carbon ones was verified, since a lower
82 amount of materials and, thus, minor costs allow for obtaining similar effectiveness to CFRP systems in
83 terms of maximum loads.

84 A few papers also report preliminary considerations regarding the theoretical prediction of the bending
85 moment of RC beams strengthened with SRP at ultimate and service loads [6,11]. Conversely, a more
86 detailed study is highlighted on the numerical simulation of the load-displacement behaviour of SRP/SRG
87 strengthened beams [12], whereas the behaviour under serviceability conditions of SRP/SRG
88 strengthened RC beams tested by Prota et al. [5] was deepened by Ceroni and Pecce [13]. These authors
89 evidenced: a) the comparable behaviour between SRP and CFRP strengthened RC members, when
90 characterized by equivalent amount of external reinforcement, and b) the more deformability exhibited by
91 members strengthened with SRG sheets with respect to those upgraded with SRP.

92 Finally, some field applications have been also performed. In particular, an experimental study performed
93 by Casadei et al. [14], explored the efficiency of the SRP systems in increasing the flexural strength of
94 “double T” prestressed RC beams which were extracted from a decommissioned two-storey parking
95 garage.

96 Lopez et al. [15], instead, proved that the application of the SRP strengthening to a concrete bridge
97 structure has the potential to be a reliable and relatively easy-to-install technique; also they pointed out
98 that the design procedure for SRP systems is comparable to that suggested by the Guide ACI 440 for FRP
99 materials in force in 2007 [16]. In this regard, it can be reasonable to assume that the failure of an RC
100 member strengthened with adhesively bonded steel fiber system, independently on the type of matrix
101 (epoxy or cementitious), is attributable to concrete crushing (when the ultimate concrete compressive
102 strain is reached) or to the failure of the composite system; the latter, in turn, can be due to the rupture of
103 the fibers in tension or to the debonding mechanism which abruptly occurs with the detachment of more
104 or less large concrete thickness. Therefore, the effectiveness of SRP/SRG systems in increasing the
105 flexural response of RC members may significantly depend, from one side, on the bond behaviour at the
106 concrete/reinforcement interface (that is mostly related to the matrix type) and, from the other side, on the
107 efficiency of the used matrix (mainly the inorganic one) to impregnate the steel fabric.

108 With the aim to better focus on these two key aspects, the experimental study presented in this paper
109 contributes to increase the current knowledge on the flexural behaviour of RC members strengthened with
110 steel fiber sheets. In particular, the work deeply analyzes the results of 10 four-point bending tests
111 performed on RC slabs strengthened with galvanized steel fiber tapes applied by using epoxy resin (SRP
112 system) or thixotropic mortar (SRG system).

113 The main study parameters were: the number of layers (1 or 2); the different density of the steel tape
114 (denoted as low, medium or high); the typology of reinforcement’s application (from the top, by turning
115 upside the slabs, or from the bottom, by placing them on a scaffold).

116 Test results have provided valuable information in terms of maximum forces, specimens’ deformability,
117 measured strains and curvatures which, coupled with the observed failure modes, are fundamental for a
118 subsequent definition of an accurate design procedure for RC beams/slabs strengthened with SRP/SRG
119 systems. To this purpose, it is highlighted that the bending tests presented herein are part of a wider
120 experimental campaign also including several bond tests performed on SRG/SRP sheets adhesively

121 connected to concrete blocks; such tests, whose results are under publication, will allow for a more
122 specific evaluation of the concrete/SRG (or SRP) interface behaviour, on which only few papers are
123 actually available in literature [6,17,18].

124 The experimental evidence has also allowed for verifying the good performance of the SRG systems,
125 whose effectiveness was not reduced by applying the strengthening system from the bottom, i.e., after
126 having placed two slabs on a scaffold (at an height of about 1.80 m from the floor), in order to simulate
127 the typical working operations found in the field.

128 Finally, preliminary analytical studies were performed to investigate the possibility of extending to the
129 SRP/SRG systems the applicability of formulations devoted to the flexural strengthening of RC members
130 with FRP sheets which are currently reported in both the Italian Guidelines CNR-DT200 R1 [1] and the
131 American ones ACI 440.2R [2].

132

133 **2. Experimental program**

134 The experimental campaign was carried out at the Laboratory of “Materials and Structural Testing” of the
135 University of Salerno (Italy) and consisted of four-point bending tests performed, in displacement control,
136 on 10 large-scale RC one-way slabs. Of these, 9 specimens were variably strengthened in bending by
137 using SRG or SRP systems, whereas the remaining one, unstrengthened, was used as benchmark.

138 Detailed information about the geometry of the tested specimens, the strengthening layouts and the test
139 set-up is reported in the following sections.

140

141 **2.1 RC specimens**

142 Figure 1 shows the geometry and the steel reinforcement of the RC slabs subjected to bending tests. As
143 illustrated, the specimens have a total length of 3700 mm and a 400 x 200 mm² rectangular cross-section;
144 the shape of the cross-section, already considered by other authors [5], is representative of shallow beams
145 found in a real structure where the effectiveness of the external SRP reinforcement can be fully exploited.

146 The longitudinal reinforcement of specimens consists of deformed steel rebars with 10 mm diameter (&).

147 In particular, five (5&10) and two (2&10) rebars made of steel grade “B450C” [19] have been used on the

148 tension and compression side, respectively; on both ends, a concrete cover of 33 mm has been considered.

149 The transverse reinforcement is constituted by steel stirrups with 8 mm diameter and 100 mm spaced.
150 Such reinforcement was designed with the aim to avoid that, in presence of SRG/SRP external
151 strengthening, the shear failure of the beams might occur before the flexural one.

152 Compression and splitting tests were carried out for the mechanical characterization of concrete's
153 properties.

154 The compression tests were performed on eight cubic 150 mm side specimens taken during the slabs'
155 manufacturing and cured under the same environmental conditions. It is highlighted that, although the 10
156 slabs were cast in two different days (in particular, 5 slabs per day), the compression strengths found from
157 the cubic specimens belonging to the two slab's series and tested at about after 4 months' curing, were
158 very similar to each other. Therefore, a unique average value of the cubic compression strength (R_{cm}),
159 equal to 18.24 MPa, can be considered for the two slabs' series, which is associated to a coefficient of
160 variation (CV) of 0.04; the corresponding cylindrical compression strength, $f_{cm} (= 0.83 R_{cm})$, is equal to
161 15.14 MPa. The motivation for selecting a concrete mix characterized by a medium-low concrete strength
162 lies in the authors' plan of simulating the experimental behaviour of beams belonging to existing
163 structures built in Italy in the '60s and '70s, i.e., when these structures were frequently manufactured
164 using low-performance concrete.

165 The splitting tests were performed on six concrete samples with 95 mm diameter and 95 mm height,
166 which were extracted from three tested slabs; in particular, a couple of concrete cores per considered slab
167 were extracted. The average value of the cylindrical tensile strength (f_{ctm}) estimated from these tests was
168 equal to 2.60 MPa, with a CV value of 0.12; it is highlighted that such an experimental data is
169 significantly higher than the value analytically calculated, for an f_{cm} value of 15.14 MPa, by applying the
170 formulations reported in the Italian Building Code [19].

171 The mechanical properties of steel rebars used as longitudinal and transverse reinforcement were
172 determined from tensile tests performed on small samples. Figure 2 shows the experimental stress-strain
173 behaviours found from these tests (three tests were performed on $\phi 10$ rebars and five tests on $\phi 8$
174 specimens), whereas the related mechanical properties are summarized in Table 1. It is first highlighted
175 that all the experimental curves do not exhibit a clearly recognizable yielding condition, and the values of
176 yield strength (f_y) listed in Table 1 are those suggested by the authors for the used rebars. Other
177 information provided in Table 1 is: the ultimate strength (f_t); the hardening ratio (f_t/f_y); the ultimate strain

178 (ϵ_i) corresponding to f_i ; finally, the last four columns of the table report the average values of the
179 mechanical properties calculated for each set of steel reinforcement ($f_{y,m}$; $f_{t,m}$; $(f_t/f_y)_m$; $\epsilon_{t,m}$).

180

181 **2.2 Strengthening materials**

182 Table 2 provides the main information related to the strengthening materials examined in the
183 experimental campaign. In particular, they are unidirectional sheets made of high strength steel cords
184 obtained by twisting steel wires within a micro-fine galvanized coating. Such products, manufactured by
185 Hardwire LLC [20], were applied underneath the beams (via wet lay-up) by using a thixotropic mortar
186 (“SRG system”) or a mineral epoxy adhesive (“SRP system”), which are both produced in Italy by
187 “kerakoll S.p.A.” [21].

188 Within the tape, the single cord is typed as “3x2”, being made of five filaments: three of these are straight
189 and are wrapped by the other two filaments at a high twist angle. Depending on the number of cords
190 distributed in the tape width, it is possible to define different densities of the reinforcement material. As
191 observed from Table 2, three tape densities (ρ) were examined in the experimental campaign, labelled
192 “GeoSteel G600”, “GeoSteel G2000” and “GeoSteel G3300” (in increasing order of the density); it is
193 noted that the number characterizing each label identifies, approximately, the weight of each tape
194 expressed in g/m^2 . For the sake of simplicity, the three densities are indicated herein as low (“LD”),
195 medium (“MD”) and high (“HD”).

196 In regard to the inorganic matrix used to obtain the SRG strengthening system, an eco-compatible
197 thixotropic mineral mortar (called “Geolite®”) has been considered, which is characterized by a very low
198 content of petrochemical polymers, and free from organic fibers. According to the manufacturer [21], the
199 product is an eco-friendly geo-mortar (of alumino-silicate nature) with a crystalline reaction geo-binder
200 base, which is recyclable and characterized by reduced CO_2 emissions and very low volatile organic
201 compounds.

202 Conversely, the organic matrix employed to yield the SRP strengthening system is a thixotropic epoxy
203 mineral adhesive. According to the manufacturer, it is solvent-free and characterized by very low volatile
204 organic compound emissions, with 46% natural mineral content. Table 2 provides the main mechanical
205 properties of the two considered impregnating matrices as resulting from the technical sheets provided by
206 the supplier [21].

207 In regard to the characterization of the steel textile used to strengthen the slabs, instead, Table 2 also
208 reports the average values of the relevant mechanical properties obtained from tensile tests performed
209 during a previous experimental campaign on the same steel tapes investigated herein [22].

210

211 **2.3 Test matrix and specimen preparation**

212 Table 3 reports the test matrix considered for the experimental campaign. In particular, each specimen is
213 identified by a label providing the following information: strengthening system (SRP or SRG), number of
214 sheet layers (1 or 2) and tape density (LD, MD or HD). As an example, the label “SRG-1LD” denotes the
215 slab strengthened by using a single layer of low density steel tape impregnated with inorganic matrix.

216 The label “US”, instead, denotes the unstrengthened specimen, i.e., the “control member” used as
217 comparison term for investigating the performances of the considered strengthening techniques.

218 As observed from Table 3, three slabs were strengthened with SRP systems and six slabs with SRG ones.

219 In the case of SRP systems, all the three tape densities, applied in a single layer, were investigated. In the
220 case of SRG systems, instead, only low and medium tape densities (applied in a single or double layer)
221 were considered because, unlike the high density, they better allow for the matrix to penetrate through the
222 sheet and create a stronger bond. Also, it is worth highlighting that the particular cord geometry (type
223 “3x2”) allows for an improved adhesion and mechanical lock between the grout and the steel cords.

224 The strengthening with double SRP layer (see specimens “SRG-2LD” and “SRG-2MD” in Table 3), was
225 obtained by overlapping two steel tapes with same length ($L_s = 2700$ mm), width ($b_s = 200$ mm) and
226 equivalent thickness ($t_{eq} = 0.084$ mm and $t_{eq} = 0.254$ mm for low and medium density, respectively); then,
227 the installation was performed by trying as much as possible to preserve the same cord spacing of the
228 single layer reinforcement. Finally, except for the specimens “SRG-1MD-A” and “SRG-1MD-B”, the
229 installation of the strengthening sheet in the laboratory was performed, for practical reasons, by turning
230 upside the tensile end of the slab and working from the above (Fig. 3). However, to check for any
231 reduction of effectiveness when the SRG external reinforcement is installed – as in the real applications –
232 from the bottom, the application of the steel tape on the slabs SRG-1MD-A and SRG-1MD-B was
233 performed after placing these two specimens on a scaffold at a height of about 1.80 m (Fig. 4). Indeed, it
234 is mentioned that the inorganic matrix requires a curing time of about 28 days in order to fully exploit its
235 effectiveness and, throughout this time, local micro-cracks or partial detachments also caused by the

236 weight of the tape, may reduce the efficiency of the reinforcement.
237 Figure 3 shows some relevant steps related to the typical application of the SRG system on the concrete
238 substrate. In particular, the first one is consisted of making the concrete surface rather rough by using a
239 mechanical hammering (Fig. 3a).
240 With the aim to assure an accurate application of the strengthening system, before applying a first layer of
241 mortar, a sort of template, about 5 mm thick, was arranged on the specimen (Fig. 3b). First, the concrete
242 surface was abundantly wetted with water (Fig. 3c) and, then, covered by a first layer of mortar (Fig. 3d).
243 Once applied the tape (Fig. 3e), a second layer of mortar was added (Fig. 2f) and, then, the top layer of
244 the package was wetted again (Fig. 3g). At the completion of these working operations, the strengthened
245 specimen has been wrapped by a nonwoven fabric and by a plastic sheet in order to assure the mortar
246 curing in moist environment (Fig. 3h).
247 The application of the SRP system, instead, did not need some of the key working operations required for
248 the SRG reinforcement, such as: impregnation of the concrete surface with water; use of proper templates
249 and protection of the specimen within the nonwoven fabric and the plastic sheet.
250 For all the strengthened members, each layer of the applied external reinforcement was 2700 mm long
251 and 200 mm wide.

252

253 **2.4 Test set-up**

254 Specimens were subjected to four-point bending tests by using a 3000 kN MTS hydraulic actuator
255 (stroke: ± 75 mm) which was mounted on a proper steel reaction frame, as shown in Figure 5.
256 Tests were carried out in displacement control (displacement rate: 0.02 mm/s), and the corresponding
257 load was measured by both using the load cell integrated in the testing machine (load capacity: 3000 kN
258 and 2500 kN, in compression and tension respectively) and an external 200 kN load cell, which assured a
259 greater accuracy for lower force values.
260 The four-point load was applied through a very stiff steel beam, capable of splitting the total load in two
261 equal forces, 960 mm symmetrically spaced with respect to the slab midspan; the clear length of the
262 simply supported slab was equal to 3400 mm, whereas the shear span measured 1220 mm.
263 Figure 6 shows the position of the two-point load and the arrangement of the measuring equipment used
264 during each test. In particular, the midspan deflection was monitored by using two potentiometers (denoted

265 with the labels “LV5” and “LV6” in Fig. 6a); in addition to these instruments, two laser sensors were also
266 considered in some tests and placed at the midspan cross-section for a better check of the vertical beam’s
267 displacement. Furthermore, other two couples of potentiometers were arranged at the slab’s center, vertically
268 spaced of about 230 mm between compression and tensile side, in order to measure a mean curvature
269 throughout the loading process. As observed in Figure 6a, the transducers “L01-FS” and “L03-RS” are
270 those placed at beam extrados, whereas “L02-FI” and “L04-RI” are the instruments located just
271 underneath the member.

272 Finally, a number of strain gauges were arranged for measuring both the compressive strain of concrete at
273 midspan cross-section (gauges “C-01” and “C-02”) and the tensile strain of steel fiber reinforcement at
274 several locations (gauges “F-01” to “F-13”, distributed according to the layout depicted in Fig. 6b).

275

276 **3. Experimental results and discussion**

277 **3.1 Failure mode and load-deflections curves**

278 Table 4 summarizes the main results obtained from the performed tests; in particular:

- 279 • F_{max} represents the peak force recorded for each specimen;
- 280 • Δ identifies the midspan deflection of each beam corresponding to F_{max} ;
- 281 • $I_{F_{max}}$ e I_{Δ} indicate, respectively, the percentage increase of force and the percentage decrease of
282 deflection calculated for each strengthened specimen with respect to the control member (US).

283 Finally, the last column of Table 4 reports the description of the failure modes observed during the tests
284 which are clearly recognizable from Figures 7-9.

285 As noted, only the specimens strengthened with a single layer of low density steel tape (i.e., specimens
286 SRP-1LD and SRG-1LD) experienced the tensile rupture of external reinforcement in the constant
287 bending moment region (Fig. 7b,c); this type of failure was observed independently on the nature of the
288 used adhesive (polymeric or inorganic). In particular, in the case of the slab SRP-1LD, the fracture
289 occurred near to the loading point “1” in Figure 6a (see Fig. 7b), whereas in the case of the test SRG-1LD
290 the phenomenon was observed at the beam’s midspan (see Fig. 7c). At the end of the loading process, the
291 two specimens exhibited a rather significant crack pattern in bending which is rather similar to that shown

292 by the unstrengthened member US (see Fig. 7a); such cracks were typically 100 mm spaced, thus
293 covering the same spacing used for transverse steel reinforcement.

294 In all the other performed tests, instead, the failure by SRP/SRG delamination from the concrete substrate
295 was always observed (Figs. 8 and 9). Such failure originally developed in the central region of each
296 member in the form of a longitudinal crack at the concrete-SRP/SRG interface; then, it rapidly propagated
297 towards one of the two slab's ends to finally cause the reinforcement peeling-off.

298 However, it is worth noting that when using the epoxy resin to apply the steel tapes, the delamination
299 clearly involved a rather significant portion of concrete substrate (Figs. 8a and 9a); when employing the
300 inorganic matrix, instead, the collapse of the composite system only partially affected the concrete
301 substrate and, conversely, it more clearly involved the mortar layer, so that an interlaminar delamination
302 in some portions of the beam took place (Figs. 8b,c and 9b).

303 The differences in the delamination mechanism observed for SRP and SRG systems is glaring in Figure 8,
304 where the slab SRP-1MD is compared with the three counterparts strengthened with the SRG
305 reinforcement (SRG-1MD, SRG-1MD-A and SRG-1MD-B). As noted, when employing the inorganic
306 matrix to bond the steel tape with medium density, the removal of a concrete thickness occurred only in
307 some portions of the slabs and, conversely, the adhesive layer kept frequently attached to the beam's
308 intrados. Also, in the case of the slab SRG-1MD, the detachment of the external reinforcement was
309 accompanied by a longitudinal fracture of the steel tape and a significant damage of the constituting cords
310 (Fig. 8b). Such damage was even more evident for the slabs SRG-2LD and SRG-2MD as shown in Figure
311 9b.

312 Disregarding the type of failure mode observed, the experimental results listed in Table 4 allowed for
313 verifying the satisfying behavior exhibited by specimens strengthened with SRG system. As observed,
314 these specimens have experienced strength increases fully comparable with those obtained in the case of
315 SRP strengthened members (for instance, comparisons between specimens SRP-1LD vs. SRG-1LD and
316 SRP-1MD vs SRG-1MD can be made).

317 Good results were also obtained by testing the specimens SRG-1MD-A and SRG-1MD-C for which, as
318 mentioned earlier, the strengthening system was applied by working from the bottom in order to simulate
319 the typical working operations found in the field (Fig. 4). As it can be observed, the two slabs showed a
320 flexural behavior comparable to that exhibited by the member SRG-1MD, which was strengthened

321 according to more “comfortable” working operations (Fig.3).

322 The comparisons in terms of load-deflection ($F-\delta$) curves obtained for all the performed tests are shown
323 in Figure 10; in Figure 11, instead, the $F-\delta$ experimental behaviors are grouped by the type of
324 strengthening system (SRP or SRG).

325 It is first highlighted that, the lower initial stiffness characterizing the $F-\delta$ curves of both control specimen
326 US and the strengthened ones SRP-1LD and SRG-1MD is due to a pre-cracking accidentally induced in
327 such beams during the transport and assembly operations.

328 Disregarding the accidental pre-cracking, the slab US showed a first loss of stiffness at a load of about 8.5
329 kN and another change in the slope of the load-deflection curve at force value of about 37.2 kN; this is of
330 course due to yielding of the tensile steel reinforcement which can be approximately estimated to occur at
331 a midspan deflection of about 24.7 mm. After this threshold, the behaviour of the specimen was
332 characterized by large flexural cracks (Fig. 7a) up to the achievement of the collapse due to concrete
333 crushing in the constant bending moment region.

334 The $F-\delta$ comparison curves show that, disregarding the nature of the matrix, the presence of the
335 strengthening system significantly increases the flexural strength of slabs. From Table 4, it is noted that
336 the percentage strength increases over the control member range from a minimum value of 27%, when
337 using a single layer of low fiber density (“LD”), to a maximum of 106% (more than doubled strength) in
338 the case of SRP system with high density sheet (“HD”). Conversely, as expected, the application of an
339 external strengthening works as an additional tensile reinforcement, thus causing a reduction of the
340 beam’s deflection measured at the achievement of the peak force. Such a reduction generally increases
341 with the amount of the external strengthening and ranges from a minimum of 29% (see the test SRG-1LD
342 in Table 4) to a maximum value of 62% (see the test SRG-1LD-B in Table 4).

343 In all the cases, at the achievement of the collapse of the steel fiber system, the $F-\delta$ curves exhibit a rather
344 abrupt strength decay and, then, the experimental responses start reproducing the typical trend of the
345 unstrengthened member (test US).

346 Figure 11 better highlights the influence of the steel fiber density and/or the number of layers for a given
347 strengthened system (SRP/SRG). In particular, Figure 11a shows significant increases of strength with the
348 sheet density; indeed, when using the medium density (test SRP-1MD), a strength increase over the test

349 SRP-1LD equal to 28% was calculated; the percentage goes up to 62% in the case of high density sheet
350 (test SRP-1HD).

351 From Figure 11b, by focusing on SRG systems, it is possible to both observe the influence of the different
352 sheet density (low and medium) and the number of layers (1 or 2). In particular, in the case of the LD
353 sheet, doubling the number of layers led to 11% strength increase (compare, for instance, SRG-1LD and
354 SRG-2LD). Such an increase is fully comparable with the performance attainable when replacing the
355 double layer of LD sheet with a single layer of MD one (compare, for instance, the specimen SRG-2LD
356 with the three slabs of type “SRG-1MD”) although the ratio between the respective sheets’ equivalent
357 thicknesses (see Table 2) is about 0.66 ($= 2 \cdot 0.082 / 0.254$). Thus, the obtained result highlights the more
358 efficiency exhibited by SRG systems made of low density steel tapes, since the higher spacing between
359 the steel cords promotes the mortar penetration and create an improved bond.

360 Finally, in regard to the installation of the medium steel fiber density, the application of two layers (test
361 SRG-2MD) allows for increasing the flexural strength over the use of the single one (tests of “SRG-
362 1MD” type) of about 29%.

363

364 **3.2 Local readings of the SRP and SRG strains**

365 As mentioned earlier, the tensile strains in the strengthening sheet were locally monitored during each test
366 by means of 13 strain gauges, arranged on the outer mortar layer of the reinforcement according to the
367 scheme illustrated in Figure 6b.

368 Figures 12 to 14 show, for some of the tested slabs, two different graphs: in the first one (Figs. 12a to
369 14a), the experimental SRP/SRG strains were plotted as a function of the total load up to achievement of
370 the maximum force F_{max} (in some cases the strain gauges stopped working before F_{max}); in the second one
371 (Figs. 12b to 14b), instead, the strain profiles along the strengthening sheets (which were 2700 mm long)
372 were plotted at some levels of the acting load, which correspond to percentage values of the peak force.
373 The denomination “central region” identifies the beam’s zone subjected to constant bending moment,
374 which was monitored by strain gauges F-04 to F-10 (see Fig. 6b). In particular, the strain gauges F-04/F-
375 05 and F-09/F10 are the couples of sensors placed on the SRG/SRP sheet where the loading points 1 and
376 2 (in Fig. 6a) were located; as such, these two point data delimiting the “central region” have been

377 obtained by averaging the readings of strain gauges F-04/F-05 and F-09/F10.

378 In Figure 12, the experimental diagrams obtained for the slab SRP-1LD are compared with the
379 corresponding plots obtained for the counterpart SRG-1LD. By looking at the strain profiles, it is
380 observed that, as expected, the maximum strains were recorded in the constant bending moment region,
381 but a more regular strain distribution along the reinforcement is observed in the case of the SRP-
382 strengthened slab. Of course, this evidence is also motivated by a non-negligible difficulty experienced in
383 measuring the strain in the SRG systems by strain gauges. Indeed, as mentioned earlier, the sensors were
384 installed on the outer portion of the external reinforcement, where a layer of mortar covers the steel tape;
385 as a result, any micro-cracks induced in the grout during the loading process, eventually developed at
386 strain gauges' location, might have affected the strain reading, and more irregular profiles or lower values
387 might have been recorded. To this purpose, it is observed that, although in terms of flexural strength SRP
388 and SRG systems employing one layer of low density tape gave rise to comparable results (Table 4), the
389 measured SRP strains are generally greater than the SRG ones at any given load level. Differences are
390 also noted from the load-SRP/SRG strain curves; in particular, in the case of the SRP-strengthened slab,
391 trilinear relationships are approximately recognized for the strain measures recorded by gauges F-04 to F-
392 10, with a significant increase of the strain rate at the achievement of the yielding condition (Fig. 12a).

393 In the case of the SRG strengthened specimen, instead, more complex trends are identified, with
394 reductions of the strain rate recorded by some gauges before the achievement of the yielding condition
395 (Fig. 12b).

396 As observed, the considerations drawn from Figure 12 can also be extended to the plots shown in Figure
397 13, related to the SRG/SRP systems employing one layer of medium density steel tape; for the sake of
398 brevity, in this Figure only the strain profiles have been reported for the specimens SRG-1MD-A and
399 SRG-1MD-B.

400 The graphs shown in Figure 14, referring to the slabs SRP-1HD, SRG-2LD and SRG-2MD, again
401 confirm a more regular trend in the strain profile corresponding to the SRP system; the strain values
402 increase by approaching the null shear region and are approximately constant in that zone, as expected.

403 Finally, Table 5 summarizes for each test the strain values recorded along the SRP/SRG sheet near the
404 achievement of load peak (F_{max}); the maximum strain measured for each test has been highlighted in
405 italics. Also, the last column of Table 5 reports the average strain values calculated in the portion of the

406 slab subjected to constant bending moment (i.e., by considering the readings performed by strain gauges
407 F-04 to F-10).

408 As noted from Table 5, by considering the same steel fiber tape, the strain values recorded for the SRP
409 systems in the constant bending moment region are slightly higher than those measured for the SRG ones.
410 For instance, for the tests SRG-1LD and SRP-1LD the calculated average strain values are equal to 0.95%
411 and 1.34%, respectively; the corresponding maximum strains are 1.49% for the SRG system (strain F-09)
412 and 1.58% for the SRP one (strain F-08), which are both close to the ultimate strain value of the steel tape
413 reported in the technical documents provided by the supplier or experimentally found (see Table 2); this
414 evidence represents a further confirmation of the failure mode experienced during these two tests, i.e. the
415 SRP/SRG fracture in the central region of the specimens.

416 Similarly, a comparison between the test SRP-1MD and the three tests of type “SRG-1MD” can be made;
417 for the former, the average strain value calculated in the beam’s central region is equal to 0.95%, whereas
418 the corresponding value recorded for the SRG system (using the MD tape) is equal to about 0.69. As it
419 can be observed, the maximum strains are rather similar to each other, by approaching the value of 1%.

420

421 **3.3 Curvatures, mean strains and neutral axes at slabs’ midspan**

422 As described in §2.4, two couples of potentiometers were arranged at the midspan of each slab, 230 mm
423 vertically spaced between compression and tensile side, in order to measure a mean curvature throughout
424 the loading process (see transducers “L01-FS”/“L03-RS” and “L02-FI”/“L04-RI” in Figure 6a). By
425 assuming a linear distribution of the strain through the cross-section (i.e. “plane section conservation”),
426 the mean curvature (χ_m) has been evaluated by using the following simplified relationship:

$$\chi_m = \frac{|\varepsilon_m^{top}| + |\varepsilon_m^{bot}|}{s_2} = \frac{(|d_m^{top}| + |d_m^{bot}|)/s_1}{s_2} \quad (1)$$

427 where d_m^{top} and d_m^{bot} represent, respectively, the mean shortenings and elongations measured by the two
428 couples of potentiometers spaced at $s_2=230$ mm, whereas the corresponding mean strains at compression
429 (ε_m^{top}) and tension (ε_m^{bot}) sides were computed on a measure length of such potentiometers (s_1) equal to
430 120 mm.

431 Figure 15 shows the experimental relationships between the bending moment and the curvature at

432 midspan for some of the tested slabs. As expected, the curves of the strengthened beams can be
433 approximated by trilinear relationships defined through the cracking, yielding and ultimate condition. By
434 focusing on the ultimate stage, characterized by the achievement of the maximum bending moment (M_{max}
435 $= F_{max}/2 \cdot L_s$), it is observed that the corresponding curvature ($\chi_{m,max}$) reduces at increasing the amount of
436 the external reinforcement. It is also noted that, for a given tape density, the maximum curvatures
437 estimated for the SRG systems are higher than the corresponding ones computed for the SRP systems
438 (compare tests SRG-1LD & SRP-1LD; tests SRG-1MD, SRG-1MD-A, SRG-1MD-B & SRP-1LD).

439 As an alternative to the experimental measure provided by strain gauges, the readings of the
440 potentiometers can be used (by always considering the “plane section conservation”) to obtain a further
441 estimate of the compression strain of concrete in compression (ϵ_c) and of SRP/SRG strain in tension (ϵ_s).

442 To this purpose, Figure 16 provides, for some representative tests, the comparison between the concrete
443 and SRP/SRG strain estimated by using the abovementioned potentiometers (labeled “SRP/SRG strain”
444 and “concrete strain” in Fig. 16) and the corresponding local strains recorded by averaging the strain
445 gauges C-01/C-02 on the compression side (in some cases C-01 was not working and only the strain
446 gauge C-02 was considered), and F-06/F-07/F-08 on the tensile side (the experimental mean curve is also
447 plotted); such strains have been plotted as a function of the bending moment acting in the “central region”
448 of the slabs. By observing these plots, it is highlighted that, in terms of compression strains, the
449 experimental curves provided by potentiometers “L01-FS”/“L03-RS” generally overlap the measures
450 obtained by strain gauges. In terms of tensile strains, instead, the measures recorded by strain gauges are
451 always lower than that obtained by potentiometers when the slabs are strengthened with SRG systems;
452 this evidence may again validate the consideration on the difficulty of measuring the local SRG strains
453 through strain gauges, being placed on the mortar layer which is significantly affected by the undergoing
454 local damage. Conversely, no specific issues seem to rise in the case of epoxy-bonded steel tapes, as
455 observed for the tests SRP-1LD and SRP-1MD. In particular, for the latter test, a perfect matching is
456 noted between the measure provided by strain gauges and that estimated by potentiometers, whereas for
457 the test SRP-1LD the local strain is even greater than mean one.

458 A further comparison between the local measure provided by the strain gauges and the mean one recorded
459 by the used potentiometers can be performed in terms of neutral axes evaluated at beam’s midspan, as
460 shown for some tests in Figures 17 and 18. In particular, Figures 17a and 18a depict the depth to the

461 neutral axis (y_c) at some percentage levels of the acting load estimated through the main strains at
462 compression and tensile side of the midspan cross-section provided by potentiometers. In Figures 17b and
463 18b, instead, the depth to the neutral axis has been plotted by considering, at the tensile side of the cross
464 section, the SRG/SRP mean strain provided by gauges F-06, F-07, F-08; at the compression side, the
465 strain measure deduced from the potentiometers “L01-FS” and “L03-RS” has been considered since, as
466 shown in Figure 16, was quite similar to that provided by gauges C-01 and C-02.

467 The depths to the neutral axis estimated at the achievement of the peak load (labeled $y_{c,A}$ and $y_{c,B}$ for the
468 neutral axes of Fig. 17a-18a and 17b-18b, respectively) are also compared in Table 5 with the
469 experimental measures ($y_{c,1}$; $y_{c,2}$; $y_{c,3}$) performed at the peak load during the tests, by considering the
470 vertical propagation of three cracks developed approximately at beam midspan (see the picture reported
471 in Table 5); the average value obtained from the three local measures ($y_{c,m}$) is also provided. As expected,
472 the estimate of the neutral axis’s depth is sensitive to the type of measure performed at the tensile side of
473 the cross-section. Specifically, by providing a strain averaged on a gauge length $s_1 = 120$ mm, the measure
474 recorded by the potentiometers is significantly affected by the number of cracks distributed within such
475 length; therefore, the value of d_m^{bot} in Eq. (1) and, consequently, of ε_m^{bot} , increases with the level of
476 cracking catch by these devices. As a result, the depths to the neutral axis listed in Table 5 ($y_{c,A}$), except
477 for one examined case (i.e., test SRP-1LD), are generally lower than the values estimated by using the
478 local strain measures provided by the strain gauges at the tensile side ($y_{c,B}$). Therefore, the choice of using
479 the SRP/SRG strain provided by the strain gauges seems to be preferable, although in some cases may
480 cause an underestimate of the effective strain exhibited in the strengthening systems, mainly for the SRG
481 ones.

482

483 **4. Analytical predictions at ultimate limit state**

484 As mentioned earlier, no international guidelines are currently available to civil engineers for estimating
485 the flexural strength of RC beams/slabs externally strengthened with either SRP or SRG systems.
486 However, the experimental tests have highlighted that the flexural behaviour of slabs reinforced with SRP
487 composites can be reasonably comparable to that experienced by CFRP-strengthened members; indeed,
488 the performed laboratory tests have highlighted that, when the SRP debonding governed the failure of the
489 slabs (see tests SRP-1MD and SRP-1HD in Figs 8a and 9a), the mechanism occurred similarly to what

490 known in literature for CFRP systems, i.e., with the removal of a significant concrete's layer underneath
491 the beams.

492 In the case of SRG systems, instead, the experimental evidence pointed out that the debonding failure of
493 the composite system only partially involves the concrete substrate and, conversely, more clearly affects
494 the grout layer. As a result, unlike the SRP applications, the debonding mechanisms governing the
495 collapse of the SRG systems may not be fully predicted through analytical formulations available for
496 CFRP composite materials, but "ad-hoc" analyses are required for a better understanding of the SRG-to-
497 concrete bond behaviour.

498 Despite these considerations, the flexural strength of the tested slabs was herein estimated, as a first
499 approximation and disregarding the type of matrix (polymeric or inorganic), according to both the Italian
500 Guidelines CNR-DT200 R1 [1] and the American ones ACI 440.2R [2]; as known, these documents deal
501 with the external strengthening of RC/masonry structures with polymeric matrix-composites employing
502 carbon, glass or aramid fibers and not steel tapes.

503 In accordance with the considered guidelines, the flexural analysis of SRP/SRG strengthened members
504 was performed by using strain compatibility and force equilibrium methods. The following basic
505 assumptions were considered: 1) plane section before loading remains plane after loading; 2) perfect bond
506 existing between SRG/SRP and concrete, and between steel reinforcement and concrete; 3) tensile
507 strength of concrete is neglected.

508 For a better modelling of the concrete behaviour in compression, the stress-strain constitutive law
509 proposed by Saenz [23] was considered in place of the simplified equivalent rectangular stress-block
510 proposed by both Guidelines, where the compression strength (f_c) coincides with the experimental mean
511 value $f_{cm} = 15.14$ MPa, and the ultimate strain ϵ_{cu} is assumed to be equal to 0.4% (Fig. 19a). An elastic-
512 perfectly plastic law was chosen for simulating the behaviour of the steel rebars in both compression and
513 tension (Fig. 19b), characterized by a yield strength $f_y = 460$ MPa (which coincides with the experimental
514 mean value $f_{y,m}$ reported in Table 1) and a corresponding strain (ϵ_y) equal to 0.23%. Finally, the tensile
515 behaviour of the SRP/SRG reinforcement was assumed to be linear-elastic until the failure condition,
516 which is achieved at strength (f_{su}) and strain (ϵ_{su}) values equal to those reported in Table 2 [22].

517 By following the indications reported in the two considered Guidelines on the flexural behaviour of RC
518 slabs strengthened with FRP, and extending the basic concepts to the case of SRP/SRG systems, two

519 types of failure can be generally expected, depending on whether the ultimate concrete compressive strain
 520 (ε_{cu}) or the maximum SRP/SRG tensile strain (ε_{smax}) is reached; the latter is determined as:

$$\varepsilon_{smax} = \min(\varepsilon_{su}; \varepsilon_{sd}) \quad (2)$$

521 where ε_{sd} is the maximum strain due to intermediate debonding failure.

522 According to the American Guide ACI 440.2R [2], the ε_{sd} value can be estimated through the following
 523 formulation:

$$\varepsilon_{sd}^{(ACI\ 440)} = 0.41 \sqrt{\frac{f_{cm}}{E_s \cdot t_{eq}}} \leq 0.9 \cdot \varepsilon_{su} \quad (3)$$

524 whereas, the Guidelines CNR-DT 200 R1 [1] provide a different relationship:

$$\varepsilon_{sd}^{(DT\ 200)} = \frac{f_{sd}}{E_s} = k_q \cdot \sqrt{\frac{E_s}{t_{eq}} \cdot 2 \cdot k_b \cdot k_{G,2} \cdot \sqrt{f_{cm} \cdot f_{ctm}}} \quad (4)$$

525 In Eq. (4): f_{sd} is the strength corresponding to the debonding failure; k_q is a coefficient accounting for the
 526 load distribution (in this case, $k_q = 1$); $k_{G,2}$ ($= 0.32$) is a corrective factor calibrated on experimental
 527 results; k_b is a geometrical corrective factor depending on the ratio between the SRP/SRG external
 528 reinforcement width (b_s) and the concrete one (b) (in this case, $b_s/b = 0.5$), which is calculated by means
 529 of the following relationship:

$$k_b = \sqrt{\frac{2 - b_s/b}{1 + b_s/b}} \geq 1 \quad (5)$$

530 It is highlighted that Eq. (4) has been written herein without any reduction factor required for design
 531 purposes. Regarding the mean value of the concrete tensile strength (f_{ctm}), instead, the following
 532 formulation reported in the Italian Building Code (19) has been selected, by considering an increase of f_{ctm}
 533 by 1.2 factor ($f_{cfm} = 1.2 \cdot f_{ctm}$) to account for the tensile strength of concrete in bending:

$$f_{cfm} = 1.2 \cdot f_{ctm} = 1.2 \cdot 0.30 \cdot (f_{ck})^{2/3} = 1.2 \cdot 0.30 \cdot (f_{cm} - 8)^{2/3} \quad (6)$$

534 The analytical results obtained by applying the formulations suggested by DT200 [1] and ACI 440 [2] to
 535 all the performed tests are reported in Tables 7 and 8, respectively. In particular, the following
 536 information at ultimate limit state is reported in each Table:

537 ✓ the maximum SRP/SRG tensile strain ε_{smax} estimated for each test which always coincides with
 538 the debonding one ($\varepsilon_{smax} = \varepsilon_{sd}$);

539 ✓ the strain values of the SRP/SRG sheet (ε_s), the steel reinforcement both in tension (ε_f) and
540 compression (ε'_f) and concrete (ε_c);

541 ✓ the stress values of the SRP/SRG sheet (σ_s), the steel reinforcement both in tension (σ_f) and
542 compression (σ'_f);

543 ✓ the depth to the neutral axis (y_c);

544 ✓ the values of the maximum bending moment (M_{max}) and total force (F_{max}) estimated for each test
545 which are compared with the corresponding experimental results.

546 Finally, the last column of each Table reports the computed mean absolute percentage error (E_{rr}) between
547 the experimental and the theoretical value of the force F_{max} .

548 By comparing the theoretical results reported in Tables 7 and 8 it is highlighted that, disregarding the type
549 of formulation applied for estimating the ε_{sd} value (Eq. 3 or 4), the SRP/SRG debonding mechanism
550 always governed the failure of all the strengthened beams, with maximum strains rather similar to those
551 experimentally measured by strain gauges in the constant bending moment region (see Table 5); also, the
552 two different relationships give rise to similar values of ε_{sd} , with slightly higher strains estimated by using
553 Eq. (4).

554 By looking at the computed errors, it can be noted that the application of Eq. (4) suggested by DT200
555 generally allows for providing a slightly better prediction of the beam's flexural strength. Disregarding
556 the given guidelines, the analytical results generally well match the experimental ones in the case of slabs
557 strengthened with one layer of low and medium density steel tape, whereas provide conservative
558 predictions in the remaining cases; the major discrepancies are noted at increasing the equivalent
559 thickness of the external reinforcement, as in the cases of slabs SRP-1HD and SRG-2MD. Therefore, the
560 considerations drawn from the few experimental-theoretical comparisons, although do not allow for an
561 exhaustive analysis on the performance of the considered relationships, highlight the need to develop a
562 more accurate modelling of the concrete-SRP/SRG interface capable of better predicting the debonding
563 mechanism and, so, the flexural strength of the strengthened slabs. In particular, by focusing on Eq. (4), it
564 seems that, in the case of the SRP systems, for which the debonding mechanism is comparable to that
565 occurring for CFRP systems, a better prediction may be easily obtained by changing the value of the

566 parameter $k_{G,2}$, being a corrective factor calibrated on experimental results of FRP strengthened slabs.
567 Conversely, in the case of the SRG systems, a specific revision of Eq. (4) is required, which better
568 accounts for the differences observed in the delamination phenomenon exhibited when using the
569 inorganic matrix to bond the steel tapes.

570

571 **5. Some considerations about SRP systems**

572 In this section, some preliminary considerations related to either the shear (τ) and normal stresses (σ_n)
573 developed at the concrete/SRP interface or the longitudinal stress acting in the external reinforcement (σ_s)
574 are drawn. To this purpose, some analytical relationships found from the literature [24] or proposed by
575 the mentioned DT200 [1] and ACI 440 [2] documents – although suitable for FRP-strengthened RC
576 members – were taken into account and applied to SRP reinforcements; then, the obtained results were
577 compared with the experimental ones.

578 It is worth highlighting that the discussion presented herein is restricted only to SRP systems due to the
579 comparable debonding mechanisms activated for SRP and FRP strengthened members, as already
580 mentioned in §4. Conversely, a specific analysis is deserved to SRG systems, for which the observed
581 debonding mechanisms, also highlighted in bond tests published in [25], require an accurate study of the
582 concrete-SRG interface.

583 In particular, the study presented herein was devoted to investigate if the intermediate debonding
584 experienced during the tests can be accurately predicted by using theoretical formulations. As known, the
585 most important types of debonding failure recognizable in the case of RC members flexurally
586 strengthened with FRP (and so, with SRP) are: *a*) the plate end debonding (namely, “Mode 1” failure)
587 and, *b*) the intermediate debonding by flexural cracks (namely, “Mode 2” failure) or by diagonal shear
588 cracks (namely, “Mode 3” failure) [1].

589 Specifically, the failure Mode 1, which is activated at or near a plate end, is generally due to a
590 combination of high interfacial shear stresses τ (generally acting on a length of approximately 100 – 200
591 mm from the sheet end) and tensile stresses perpendicular to the interface between external reinforcement
592 and concrete (i.e., the normal stresses, σ_n); the latter ones may significantly arise due to the high stiffness
593 of the external reinforcement, thus reducing the allowable interfacial shear stresses, as shown by the

594 delamination circle tangential to the Mohr-Coulomb criterion failure [24]. This delamination circle is
 595 defined through a relationship between the maximum shear stress τ_{lmax} and the maximum normal
 596 (peeling) stress σ_{nmax} , which in turn can be expressed as a function of the concrete compressive strength
 597 f_{cm} and the concrete tensile strength f_{ctm} as follows:

$$\tau_{lmax}^2 = F \cdot f_{cm} \cdot f_{ctm} - F \cdot (f_{cm} - f_{ctm}) \cdot \sigma_{nmax} - F \cdot \sigma_{nmax}^2 \quad (7)$$

598 where:

$$F = \frac{f_{cm} \cdot f_{ctm}}{(f_{cm} + f_{ctm})^2} \quad (8)$$

599 and σ_{nmax} is the maximum peeling stress obtained at the sheet end, i.e., by plugging $x=0$ in Eq. (9), which
 600 is derived from a linear –elastic analysis [24]:

$$\sigma_n(x) \approx \frac{K_n \cdot M_0}{2 \cdot \beta^2 \cdot E_c \cdot I_c} \cdot e^{-\beta x} [\cos(\beta x) - \sin(\beta x)] \quad (9)$$

601 In Eq. (9):

602 - $M_0 = F/2 \cdot L_0$ is the bending moment acting at the laminate end ($x = 0$) which, in the examined cases, is
 603 located at a distance $l_0 = 350$ mm from the beam support (see Fig. 6a);

604 - E_c is the modulus of elasticity of the concrete which can be estimated according to the following
 605 formulation reported in the Italian Building Code (19):

$$E_c = 22000 \cdot \left(\frac{f_{cm}}{10}\right)^{0.3} \quad (\text{MPa}) \quad (10)$$

606 - I_c is the second moment of inertia of the concrete;

607 - β is defined by:

$$\beta = \sqrt[4]{\frac{K_n \cdot b_s}{4 \cdot E_s \cdot I_s}} = \sqrt[4]{\frac{E_a/t_a \cdot b_s}{4 \cdot E_s \cdot I_s}} \quad (11)$$

608 where E_a and t_a denote the elastic modulus and the thickness of the adhesive (epoxy) layer, and I_s
 609 represents the second moment of inertia of the SRP sheet.

610 As observed from Eq. (7), the value of τ_{lmax} significantly reduces at increasing the value of σ_{nmax} , whereas
 611 attains the maximum threshold when the acting peeling stress is equal to zero, i.e. when $\tau_{lmax} = \tau_{lm}$,
 612 corresponding to the “pure” shear condition. In this case:

$$\tau_{lmax} = \tau_{lm} = \frac{f_{cm} \cdot f_{ctm}}{f_{cm} + f_{ctm}} \quad (12)$$

613 Figure 20 shows the behavior of the peeling stress function obtained by applying Eq. (9) to the three
 614 examined cases, i.e.: test SRP-1LD, SRP-1MD and SRP-1HD. In plotting this function, a value of $E_a =$
 615 5300 MPa (see Table 2) has been assumed, whereas two different thicknesses of the adhesive layer have
 616 been considered (0.5 and 1.5 mm); furthermore, the values of $F/2 = F_{max}/2$, experimentally obtained for
 617 each test, have been plugged in Eq. (9) (see F_{max} in Table 4).

618 As observed from Figure 20, independently on the value of t_a , the σ_n function tends very quickly to zero
 619 and achieves very low values even for $x = 0$ (i.e. at the laminate end), where $\sigma_n = \sigma_{nmax}$ is equal to 0.0002
 620 MPa, 0.0013 MPa, 0.0031 MPa for specimens SRP-1LD, SRP-1MD and SRP-1HD, respectively. The
 621 very low value of σ_{nmax} (≈ 0 MPa) implies that the maximum shear stress occurring at a plate end
 622 debonding, equal to about 1.035 MPa for all the three examined cases (from Eq. 7), approximately
 623 coincides with that obtainable by considering Eq. (12), i.e., in the case of “pure” shear condition.

624 The estimated value of τ_{lmax} can be then compared with the experimental data of the interfacial SRP-
 625 concrete shear stresses calculated by using the strain gauges’ readings available in the “shear span” (see
 626 strain gauges F-01 to F-05 and F-09 to F-13 in Fig. 6b). Such experimental mean values, shown in
 627 Figures 21a, 22a and 23a for the three considered cases, have been obtained at some percentage levels of
 628 F_{max} , according to the following relationship:

$$\tau = \frac{(\varepsilon_2 - \varepsilon_1) \cdot E_s \cdot t_{eq}}{x_2 - x_1} \quad (13)$$

629 where ε_1 and ε_2 identify the strain measures recorded by two adjacent strain gauges, spaced at (x_2-x_1) .

630 As noted, in the case of the specimen SRP-1LD (Fig. 21a), the estimated value of $\tau_{lmax} \approx 1.035$ MPa is
 631 significantly higher than the experimental data plotted by using Eq. (13); this observation implies that, in
 632 such test, the debonding mechanism did not affect the collapse of the slab, as confirmed by the
 633 experimental evidence (fracture of the SRP system at the slab midspan was experienced for this test).

634 Conversely, by approaching the bending moment region, the value of τ_{lmax} is overcome in the case of the
 635 specimen SRP-1HD (Fig. 22a) and almost matched in the test SRP-1MD (Fig. 23a); therefore, the result
 636 confirms that the debonding failure took place in these two experimental tests.

637 Another consideration about the types of SRP debonding failure observed during the tests can also be
 638 performed by estimating the debonding strengths achievable in plate end debonding failure (Mode 1) and
 639 intermediate debonding by flexural cracks failure (Mode 2); to this purpose, the predictive relationships
 640 suggested by DT200 [1] and ACI 440 [2] documents have been considered.

641 In particular, according to DT200, the debonding strength in Mode 1 is given by:

$$f_{sd,mode\ 1}^{(DT200)} = \sqrt{\frac{2 \cdot E_s \cdot \Gamma_{Fd}}{t_{eq}}} \quad (14)$$

642 where Γ_{Fd} is the specific fracture energy estimated through the following relationship:

$$\Gamma_{Fd} = k_b \cdot k_G \cdot \sqrt{f_{cm} \cdot f_{ctm}} \quad (15)$$

643 where $k_G (= 0.077)$ is a corrective factor calibrated on experimental results.

644 The debonding strength due to flexural crack (Mode 2), instead, is obtained by multiplying Eq. (4) by the
 645 elastic modulus E_s :

$$f_{sd,mode\ 2}^{(DT200)} = k_q \cdot \sqrt{\frac{E_s}{t_{eq}} \cdot 2 \cdot k_b \cdot k_{G,2} \cdot \sqrt{f_{cm} \cdot f_{ctm}}} \quad (16)$$

646 Similarly, the formulation provided by ACI 440 to estimate the debonding strength in Mode 2 failure
 647 derives from Eq. (3):

$$f_{sd,mode\ 2}^{(ACI\ 440)} = 0.41 \sqrt{\frac{E_s \cdot f_{cm}}{t_{eq}}} \quad (17)$$

648 Figures 21b, 22b and 22b show, for the tests under consideration, the distribution of the longitudinal
 649 tensile stress in the SRP reinforcement experimentally computed at some percentage levels of the force
 650 F_{max} ; such values derive from the strain distributions illustrated in Figures 12-14 and multiplying them by
 651 the elastic modulus of the steel tape E_s . Also, the values of the debonding strength in both Mode 1 and 2,
 652 estimated according the mentioned Eqs. (14), (16) and (17), are shown in these plots and compared with
 653 the experimental data.

654 As observed in Figure 21b, related to the test SRP-1LD, the estimated value of $f_{sd,mode\ 1}^{(DT200)}$ is
 655 significantly higher than the maximum longitudinal stresses measured toward the sheet end, thus
 656 confirming that the failure of the slab was not governed by a such debonding mechanism. Conversely, the
 657 estimated values of $f_{sd,mode\ 2}^{(DT200)}$ and $f_{sd,mode\ 2}^{(ACI\ 440)}$ are overcome by the experimental stress values but, as

658 mentioned earlier, in this test the fracture of the SRP system at the slab midspan was experienced.
659 By observing the plot in Figure 22b and 22c, related to the tests SRP-1MD and SRP-1HD, respectively, it
660 is noted that the values of $f_{sd,mode\ 1}^{(DT200)}$ are again lower than the experimental stress data measured at the
661 sheet ends; conversely, the values of $f_{sd,mode\ 2}^{(DT200)}$ and $f_{sd,mode\ 2}^{(ACI\ 440)}$ are significantly overcome by
662 approaching the constant bending moment regions, meaning that intermediate debonding took place for
663 these specimens, as experimentally observed.

664

665 **6. Conclusions**

666 In this paper, the experimental results of four-point bending tests performed on RC one-way slabs
667 strengthened with SRP/SRG systems have been presented and discussed.

668 In addition to the nature of the used adhesive (polymeric or cementitious), the main study parameters
669 were the number of layers (one or two), the steel tape density (low, medium or high) and, in the case of
670 the SRG system, the way of strengthening installation (from the top or the bottom).

671 The performed tests have shown that, disregarding the type of adhesive, the slabs strengthened with one
672 layer of low density tape (specimens SRG-1LD and SRP-1LD) have both experienced the fracture of the
673 sheet in the constant bending moment region. In all the other cases, instead, an SRP/SRG delamination
674 failure was always observed. However, in regard to SRG-strengthened slabs, the collapse of the
675 strengthening system has significantly involved the mortar layer, whereas only a limited removal of
676 concrete substrate, concentrated in a few zones of the beam length, was experienced as otherwise
677 observed in the case of SRP systems.

678 Regardless of the observed failure mode, test results have allowed for verifying the good performance
679 exhibited by RC slabs strengthened with SRG systems which have shown strength increases comparable
680 to those obtained from companion specimens strengthened with SRP. The efficiency of the SRG system
681 was even more evident when using the low density (LD) tape, both in single or double layer; in particular,
682 the slab strengthened with two SRG layers showed an increase of strength fully comparable to that
683 provided by specimens strengthened with one layer of medium density (MD) tape, characterized by a
684 thickness of 1.5 times over that obtained with two LD layers.

685 By looking at the strain profiles plotted by using the strain gauges' readings, a more regular strain

686 distribution along the external reinforcement was observed in the case of the SRP-strengthened slabs,
687 with values that are generally greater than those measured in the SRG companion specimens. This
688 evidence was also motivated by the unquestionable difficulty in recording the strain in the SRG systems
689 through strain gauges, since any micro-cracks induced in the grout during the loading process of the slabs,
690 eventually developed at strain gauges' location, might have affected the strain reading, and more irregular
691 profiles or lower values might have been recorded.

692 Finally, preliminary analytical studies were performed for verifying, as a first approximation, the
693 possibility of extending the applicability of formulations currently reported in both the Italian Guidelines
694 CNR-DT200 R1 and the American Guide ACI 440.2R for the flexural strengthening of RC members with
695 FRP sheets; the main difference existing between the two documents lies in the formulation adopted for
696 estimating the maximum strain of the external reinforcement due to intermediate debonding failure. By
697 focusing on SRP systems only, some considerations related to either the shear and normal stresses
698 developed at the concrete/SRP interface or the longitudinal stress acting in the external reinforcement
699 were also drawn.

700 The results of the performed study have shown a slightly better prediction of the beam's flexural strength
701 obtained by using the formulation suggested by DT200. Disregarding the used guidelines, the analytical
702 results generally well match the experimental ones in the case of slabs strengthened with one layer of low
703 and medium density steel tape, whereas provide conservative predictions in the remaining cases; the
704 major discrepancies are noted at increasing the equivalent thickness of the external reinforcement.
705 However, regardless of the greater or lesser accuracy of the obtained results, the preliminary analytical
706 study has highlighted the need to develop a refined modelling of the concrete-SRP/SRG interface
707 behaviour, capable of better predicting the debonding mechanism and, so, the flexural strength of the
708 strengthened slabs. This consideration is even more relevant in the case of the SRG systems due to the
709 different delamination phenomenon exhibited when using the inorganic matrix to bond the steel tape to
710 the concrete surface.

711

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719

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777

Figure captions

Figure 1 – Geometry and the steel reinforcement configuration of the RC slabs.

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Table[Click here to download Table: Tables_June 4_2015.docx](#)

Table 1. Steel rebars' properties

Steel Reinforcement	Diameter [mm]	Test N.	f_y [MPa]	f_t [MPa]	f_t/f_y [-]	ϵ_t [%]	$f_{y,m}$ [MPa]	$f_{t,m}$ [MPa]	$(f_t/f_y)_m$ [-]	$\epsilon_{t,m}$ [%]
Longitudinal	10	1	460.1	657.2	1.43	7.16	460	655	1.42	7.72
		2	462.7	655.7	1.42	6.97				
		3	458.9	652.2	1.42	9.03				
Transverse	8	1	521.3	685.5	1.31	5.42	524	690	1.32	7.10
		2	521.5	688.6	1.32	7.38				
		3	524.5	682.7	1.30	8.41				
		4	523.5	709.8	1.36	7.68				
		5	527.0	682.1	1.29	6.62				

Table 2. Typology and mechanical properties of the used strengthening materials




STEEL TAPE					
Effective area of one cord "3x2"		$A_{\text{cord}} = 0.538 \text{ mm}^2$			
Ultimate tensile strength*		$f_{\text{su}} > 2800 \text{ MPa}$		$f_{\text{su}} = 3302 \text{ MPa}$	
Modulus of elasticity*		$E_s > 190000 \text{ MPa}$		$E_s = 206600 \text{ MPa}$	
Ultimate tensile strain		$\epsilon_{\text{su}} > 1.50\%$		$\epsilon_{\text{su}} = 1.80\%$	
<i>*Properties related to the dry sheet</i>		<i>(Data provided by supplier)</i>		<i>(Data determined experimentally [22])</i>	
Low density (LD)		Medium density (MD)		High density (HD)	
					
GEOSTEEL G600		GEOSTEEL G2000		GEOSTEEL G3300	
N. cord/mm, ρ	0.157	N. cord/mm, ρ	0.472	N. cord/mm, ρ	0.709
Weigth, w	0.67 kg/m ²	Weigth, w	2.00 kg/m ²	Weigth, w	3.30 kg/m ²
Equivalent thickness $t_{\text{eq}} = A_{\text{cord}} \cdot \rho$	0.084 mm	Equivalent thickness $t_{\text{eq}} = A_{\text{cord}} \cdot \rho$	0.254 mm	Equivalent thickness $t_{\text{eq}} = A_{\text{cord}} \cdot \rho$	0.381 mm
MATRIX (mechanical properties at 28 days of curing)					
<i>GEOLITE® – Thixotropic mineral mortar</i>			<i>GEOLITE® GEL – Epoxy mineral adhesive</i>		
Compressive strength	> 55 MPa		Tensile strength	> 14 MPa	
Tensile strength in bending	> 10 MPa		Shear strength	> 20 MPa	
Modulus of elasticity in compression	= 25000 MPa		Modulus of elasticity in compression	> 5300 MPa	

Table 3. Test matrix

Test #	Test Identification	Type of matrix	N. of layers	Tape density
1	US	–	–	–
2	SRP-1LD	polymeric	1	Low
3	SRP-1MD		1	Medium
4	SRP-1HD		1	High
5	SRG-1LD	grout	1	Low
6	SRG-2LD		2	Low
7	SRG-1MD		1	Medium
8	SRG-1MD-A		1	Medium
9	SRG-1MD-B		1	Medium
10	SRG-2MD		2	Medium

Table 4. Test results and failure modes

Test	F_{\max} [kN]	Δ [mm]	$I_{F\max}$ [%]	I_{Δ} [%]	Failure mode
US	45.23	137.61	–	–	Concrete failure in compression
SRP-1LD	57.30	86.03	26.70	-37.49	Fracture of the SRP system at the slab midspan
SRP-1MD	73.15	72.56	61.75	-47.27	SRP delamination
SRP-1HD	93.10	69.96	105.86	-49.16	SRP delamination
SRG-1LD	61.85	97.16	36.76	-29.39	Fracture of the SRG system at the slab midspan
SRG-2LD	68.70	76.28	51.91	-44.57	Delamination of the SRG system
SRG-1MD	69.55	57.10	53.79	-58.51	Delamination of the SRG system
SRG-1MD-A	70.25	53.49	55.33	-61.13	Delamination of the SRG system
SRG-1MD-B	64.28	51.79	42.12	-62.37	Delamination of the SRG system
SRG-2MD	87.58	54.65	93.64	-60.29	Delamination of the SRG system

Table 5. Strains measured in the strengthening system at the achievement peak load

Test	F _{max} [kN]	F-01 [%]	F-02 [%]	F-03 [%]	F-04 [%]	F-05 [%]	F-06 [%]	F-07 [%]	F-08 [%]	F-09 [%]	F-10 [%]	F-11 [%]	F-12 [%]	F-13 [%]	ε _{s,m} [*] [%]
SRP-1LD	57.30	0.117	0.215	0.337	1.153	-	-	-	1.582	1.374	0.268	0.484	0.242	-	1.344
SRP-1MD	73.15	0.152	0.350	0.766	0.908	1.052	1.123	0.993	0.938	0.706	0.944	0.706	0.287	0.040	0.952
SRP-1HD	93.10	0.074	0.397	0.529	0.909	0.918	0.969	0.947	0.797	0.717	0.929	0.608	0.435	0.177	0.884
SRG-1LD	61.85	0.051	0.209	0.436	0.578	1.055	1.093	0.692	0.781	1.486	-	0.576	0.386	0.105	0.947
SRG-2LD	68.70	0.131	0.269	0.679	0.834	0.505	0.808	1.073	1.015	1.022	1.037	0.642	0.254	-	0.899
SRG-1MD	69.55	-	0.178	0.448	0.667	0.667	0.728	0.765	0.455	0.799	0.663	1.287	0.221	0.131	0.678
SRG-1MD-A	70.25	0.198	0.212	0.385	0.626	0.620	0.635	0.846	0.693	-	0.728	0.535	0.257	0.066	0.691
SRG-1MD-B	64.28	0.061	0.194	0.462	0.559	1.458	0.623	0.559	0.605	0.559	0.522	0.584	0.217	0.049	0.698
SRG-2MD	87.58	0.239	0.269	0.478	0.746	0.612	0.563	0.714	0.610	0.523	-	-	-	-	0.628

* Value obtained by averaging the strain readings provided by strain gauges F-04 to F-10

Table 6. Measured and estimated values of the neutral axis's depth at the peak load

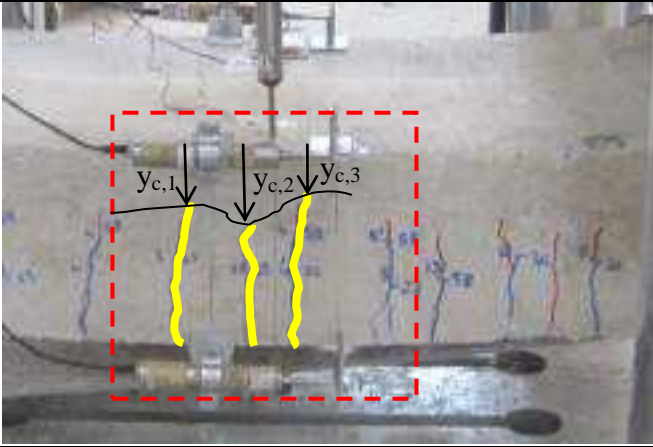
Test	<i>Measured</i>					<i>Estimated</i>	
	$y_{c,1}$ [mm]	$y_{c,2}$ [mm]	$y_{c,3}$ [mm]	$y_{c,m}$ [mm]		$y_{c,A}$ [mm]	$y_{c,B}$ [mm]
US	24.1	51.8	46.5	40.8		41.9	–
SRP-1LD	46.5	42.8	46.5	45.3		54.1	38.6
SRP-1MD	54.3	46.4	61.5	54.1		52.7	53.1
SRP-1HD	87.3	43.7	52.4	61.1		–	–
SRG-1LD	50.3	54.1	50.3	51.5		23.5	44.6
SRG-2LD	44.8	72.8	44.8	54.2		–	–
SRG-1MD	47.7	56.7	66.2	56.9		36.4	61.6
SRG-1MD-A	57.1	64.3	50.0	57.1		17.4	30.7
SRG-1MD-B	53.5	66.8	57.9	59.4		27.2	52.3
SRG-2MD	60.2	62.1	56.3	59.6		–	–

Table 7. Theoretical predictions according to CNR-DT 200 R1 [1]

Test	$\varepsilon_{s\max} = \varepsilon_{sd}$ [%]	ε_s [%]	ε_f [%]	ε'_f [%]	ε_c [%]	σ_s [MPa]	σ_f [MPa]	σ'_f [MPa]	y_c [MPa]	<i>theoretical</i>		<i>experimental</i>		E_{IT} (%)
										M_{\max} [kN m]	F_{\max} [kN]	M_{\max} [kN m]	F_{\max} [kN]	
US	–	–	–	–	–	–	460	77	33.1	27.82	45.61	27.59	45.23	0.83
SRP-1LD	1.31	1.31	1.07	0.08	0.32	2531	460	160	39.5	35.07	57.49	34.95	57.30	0.33
SRP-1MD	0.75	0.75	0.61	0.09	0.24	1456	460	184	48.0	40.16	65.84	44.62	73.15	10.00
SRP-1HD	0.62	0.62	0.49	0.09	0.22	1189	460	194	52.5	42.75	70.09	56.79	93.10	24.72
SRG-1LD	1.31	1.31	1.07	0.08	0.32	2531	460	160	39.5	35.07	57.49	37.73	61.85	7.05
SRG-2LD	0.93	0.93	0.75	0.08	0.26	1790	460	174	44.2	37.96	62.23	41.91	68.70	9.42
SRG-1MD	0.75	0.75	0.61	0.09	0.24	1456	460	184	48.0	40.16	65.84	42.43	69.55	5.34
SRG-1MD-A	0.75	0.75	0.61	0.09	0.24	1456	460	184	48.0	40.16	65.84	42.85	70.25	6.28
SRG-1MD-B	0.75	0.75	0.61	0.09	0.24	1456	460	184	48.0	40.16	65.84	39.21	64.28	2.42
SRG-2MD	0.53	0.53	0.42	0.10	0.21	1029	460	201	56.2	44.90	73.61	53.42	87.58	15.95

Table 8. Theoretical predictions according to ACI 440.2R. [2]

Test	$\varepsilon_{smax} = \varepsilon_{sd}$ [%]	ε_s [%]	ε_f [%]	ε'_f [%]	ε_c [%]	σ_s [MPa]	σ_f [MPa]	σ'_f [MPa]	y_c [MPa]	<i>theoretical</i>		<i>experimental</i>		E_{IT} (%)
										M_{max} [kN m]	F_{max} [kN]	M_{max} [kN m]	F_{max} [kN]	
US	–	–	–	–	–	–	460	77	33.1	27.82	45.61	27.59	45.23	0.83
SRP-1LD	1.25	1.25	1.02	0.07	0.31	2417	460	154	39.5	34.75	56.97	34.95	57.30	0.58
SRP-1MD	0.72	0.72	0.58	0.09	0.23	1390	460	177	48.1	39.59	64.89	44.62	73.15	11.29
SRP-1HD	0.59	0.59	0.47	0.09	0.21	1135	460	186	52.6	42.05	68.94	56.79	93.10	25.95
SRG-1LD	1.25	1.25	1.02	0.07	0.31	2417	460	154	39.5	34.75	56.97	37.73	61.85	7.89
SRG-2LD	0.89	0.89	0.72	0.08	0.25	1709	460	168	44.3	37.50	61.47	41.91	68.70	10.53
SRG-1MD	0.72	0.72	0.58	0.09	0.23	1390	460	177	48.1	39.59	64.89	42.43	69.55	6.69
SRG-1MD-A	0.72	0.72	0.58	0.09	0.23	1390	460	177	48.1	39.59	64.89	42.85	70.25	7.62
SRG-1MD-B	0.72	0.72	0.58	0.09	0.23	1390	460	177	48.1	39.59	64.89	39.21	64.28	0.96
SRG-2MD	0.51	0.51	0.40	0.09	0.20	983	460	192	56.3	44.10	72.29	53.42	87.58	17.46

Figure

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Figure 1

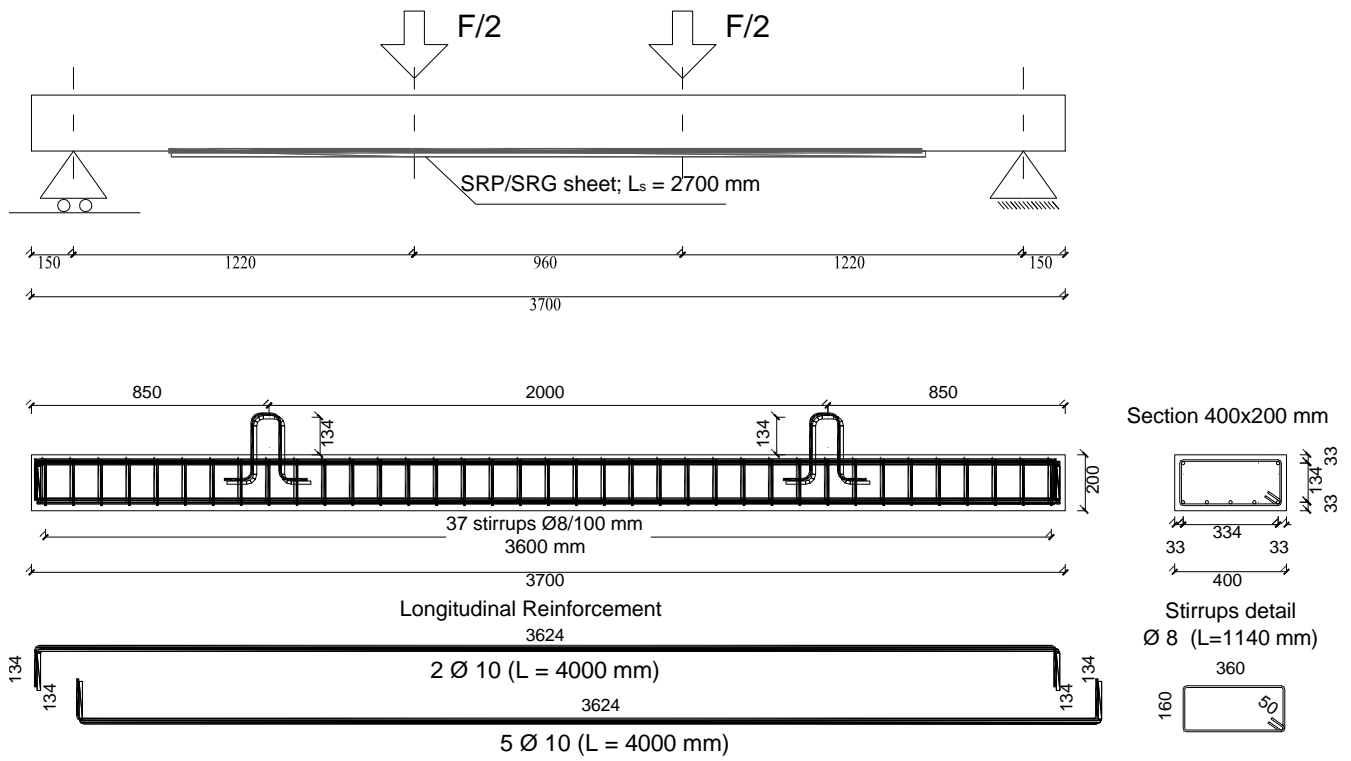


Figure 2

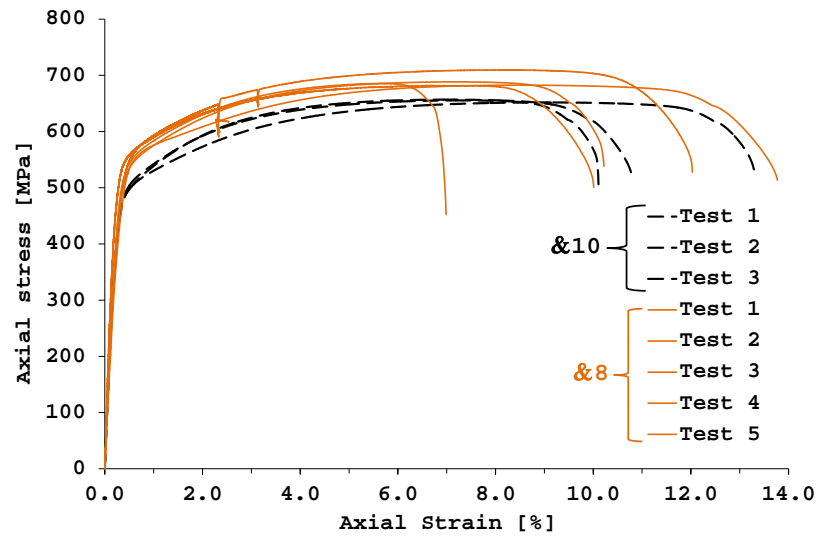


Figure 3



Figure 4

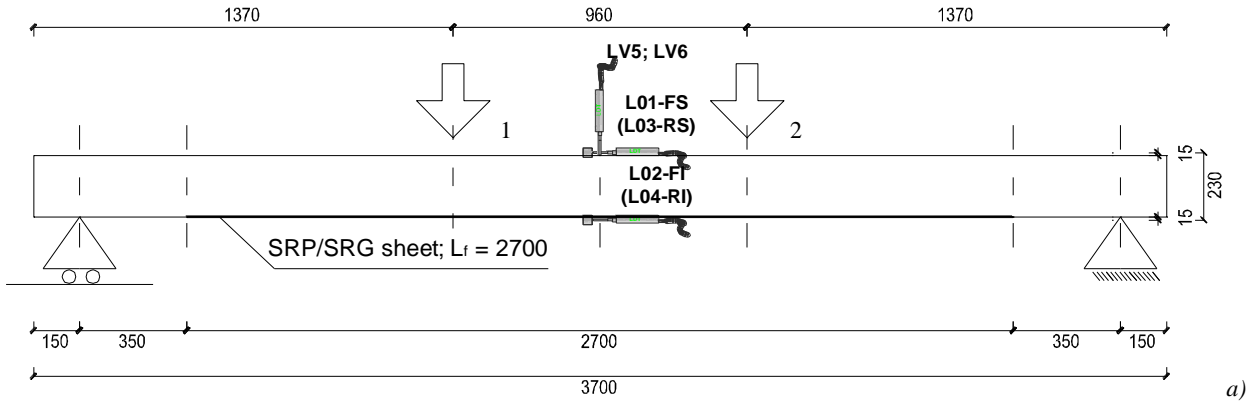


Figure 5 (only colour on the web)

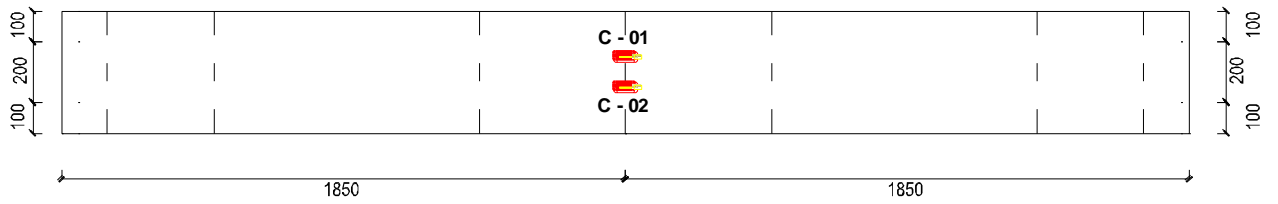


Figure 6 (only colour on the web)

FRONT VIEW



TOP VIEW



BOTTOM VIEW

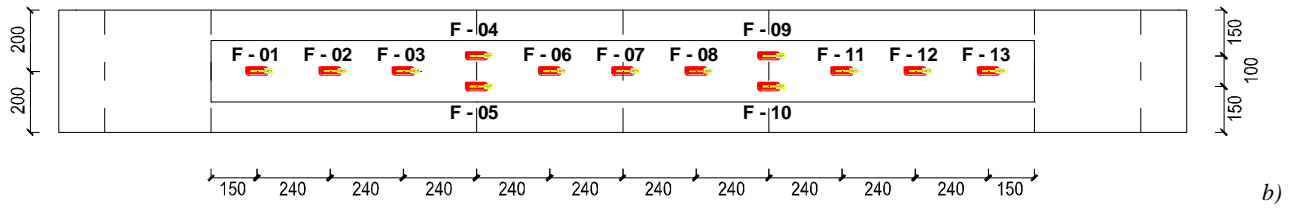


Figure 7 (only colour on the web)

a) Test US



b) Test SRP-1LD

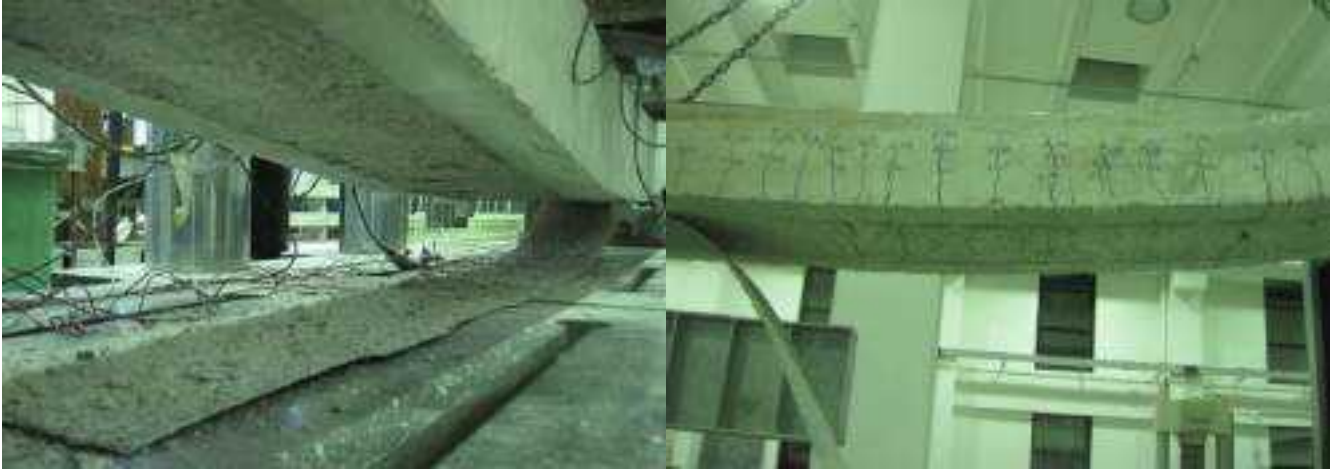


c) Test SRG-1LD



Figure 8 (only colour on the web)

a) Test SRP-1MD



b) Test SRG-1MD



c) Test SRG-1MD-A & SRG-1MD-B



Figure 9 (only colour on the web)

a) Test SRP-1HD



b) Test SRG-2LD & SRG 2MD



Figure 10 (only colour on the web)

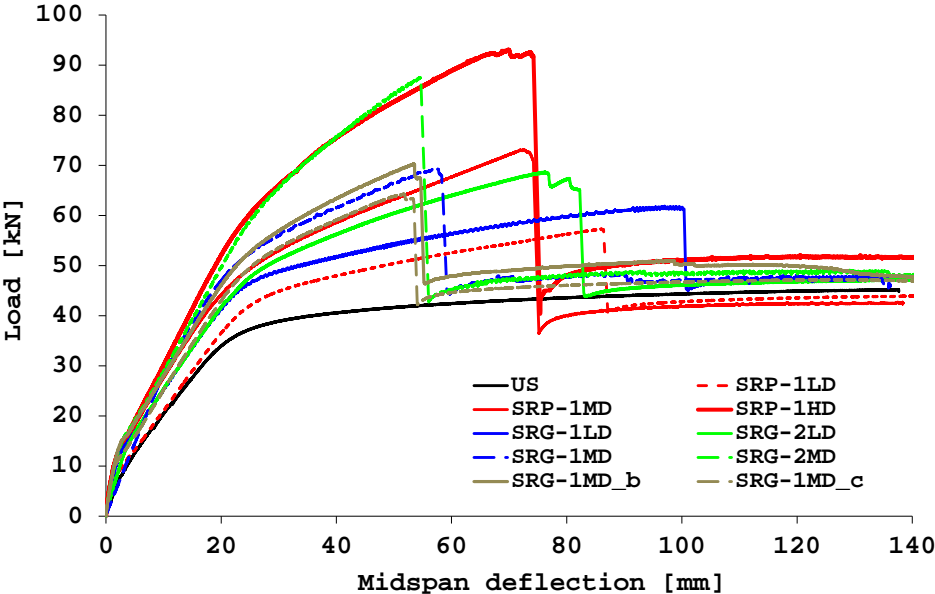


Figure 11 (only colour on the web)

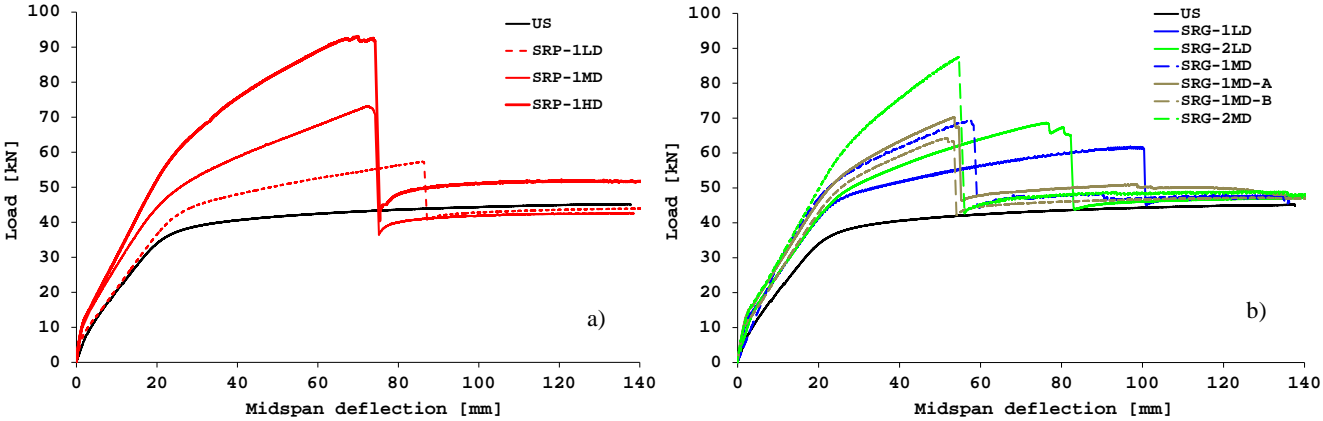
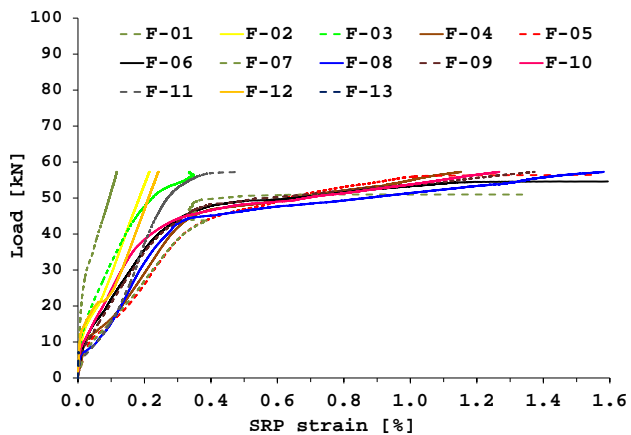
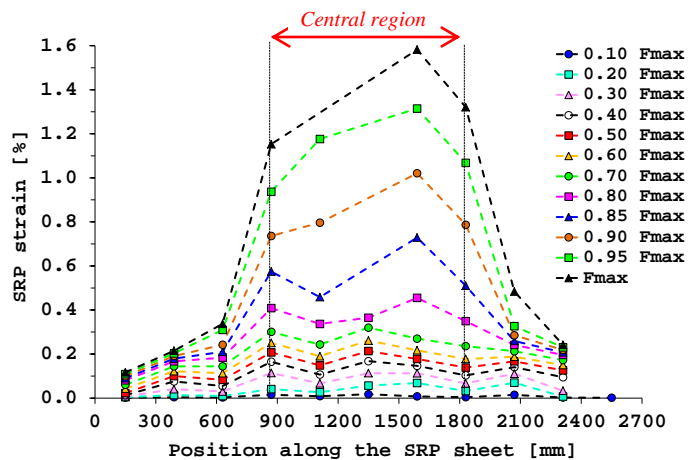


Figure 12 (only colour on the web)

Test SRP-ILD

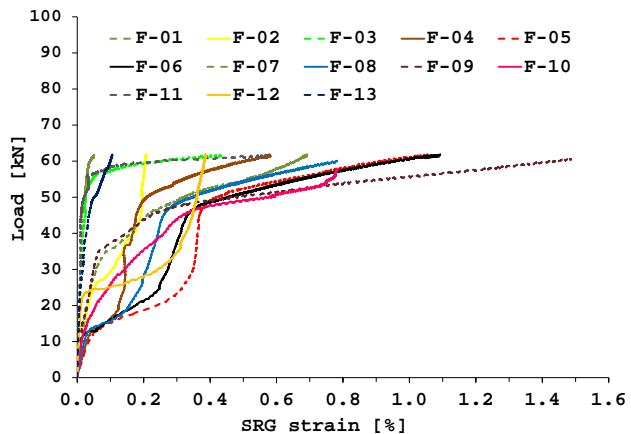


a)

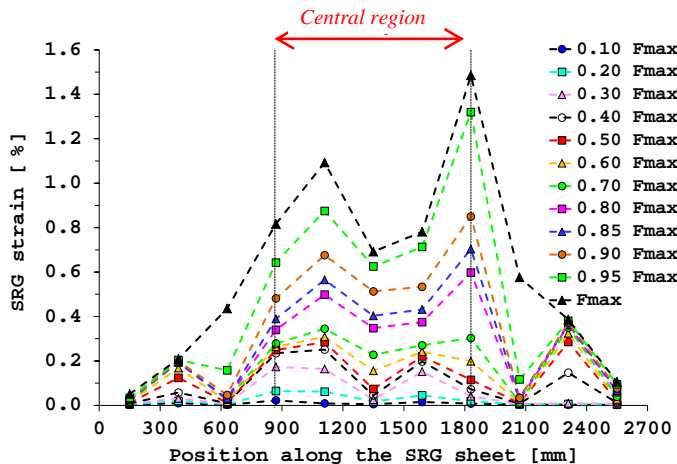


b)

Test SRG-ILD



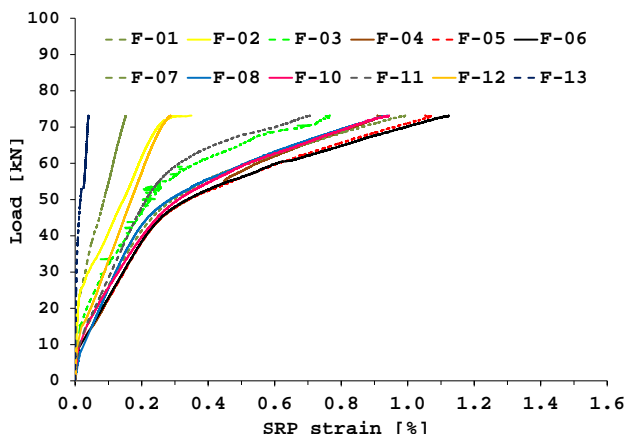
a)



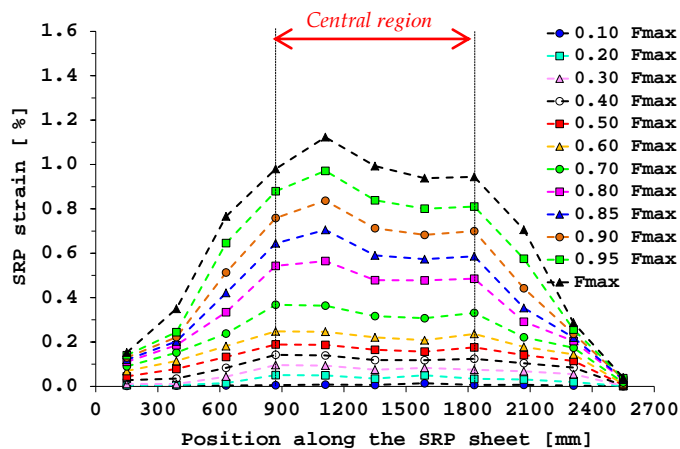
b)

Figure 13 (only colour on the web)

Test SRP-IMD

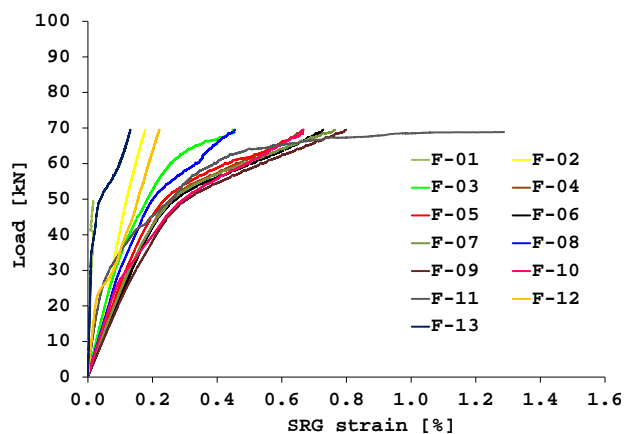


a)

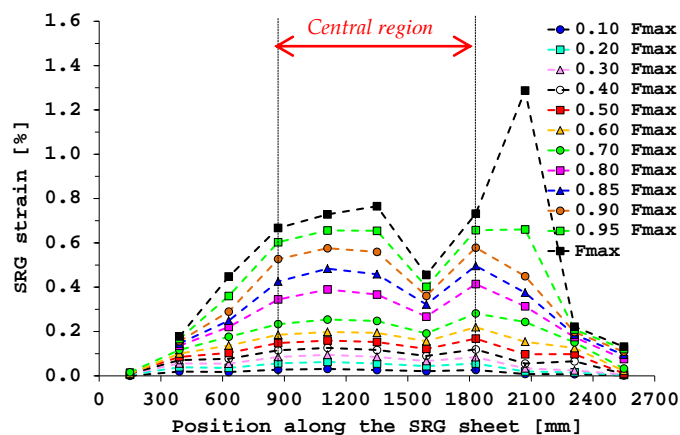


b)

Test SRG-IMD

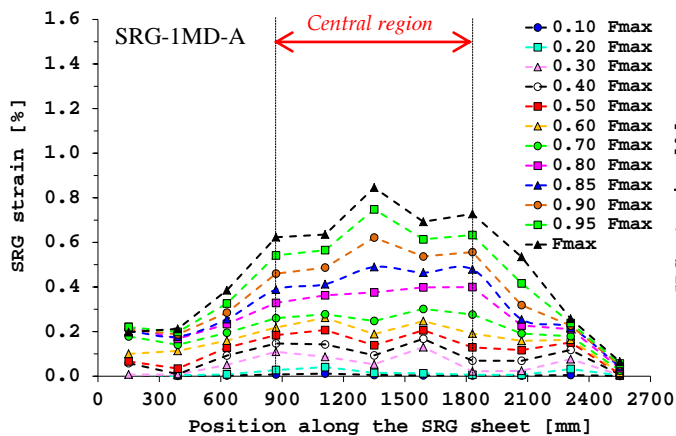


a)

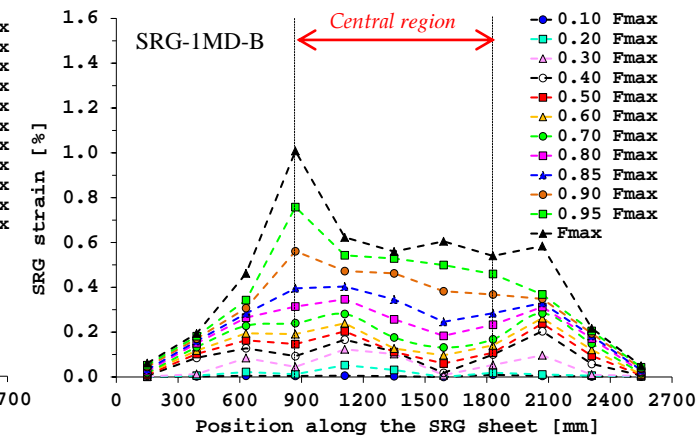


b)

Test SRG-IMD-A & SRG-IMD-B



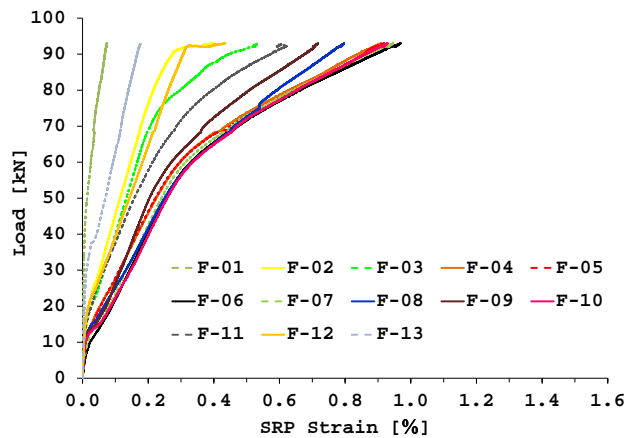
b)



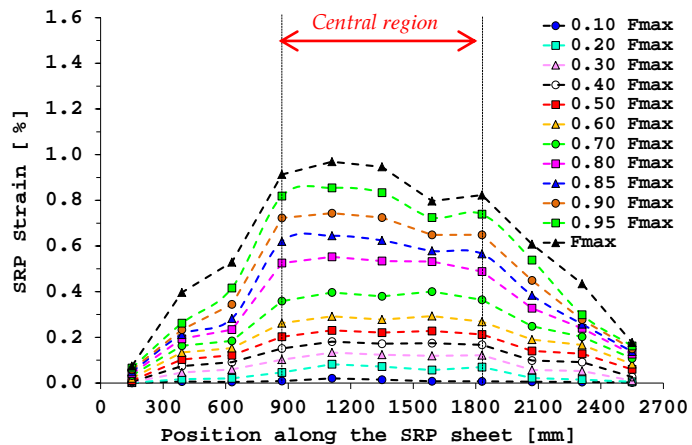
b)

Figure 14 (only colour on the web)

Test SRP-1HD

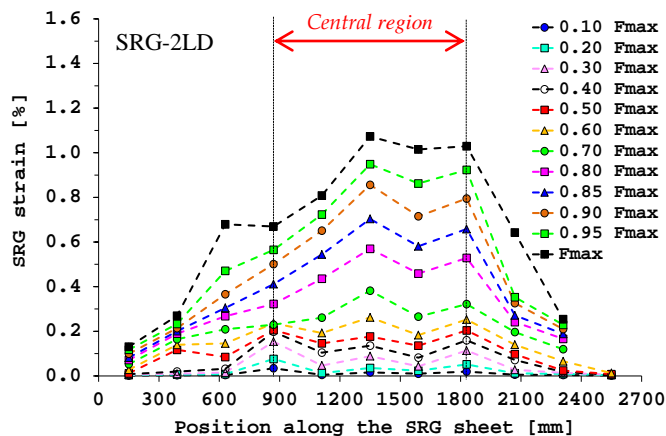


a)

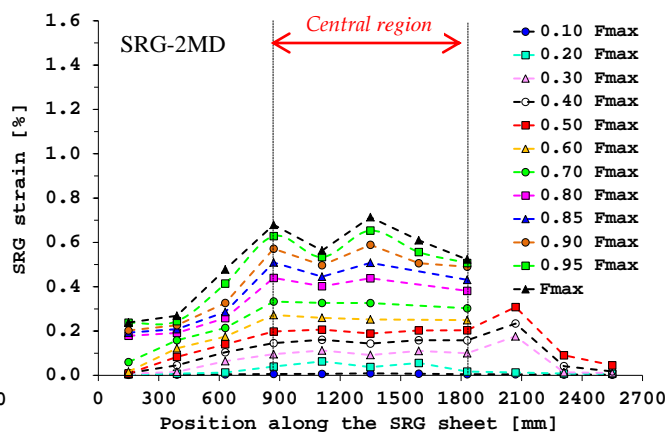


b)

Test SRG-2LD & SRG 2MD



b)



b)

Figure 15 (only colour on the web)

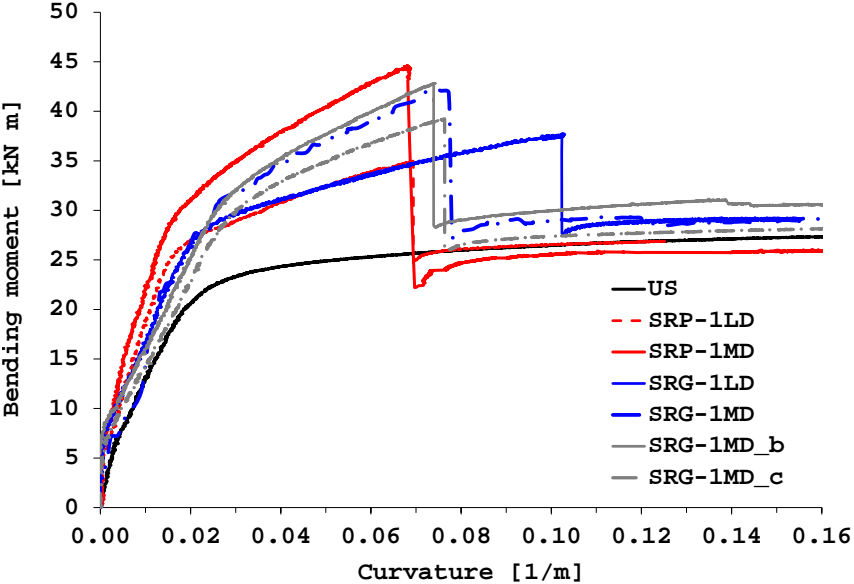
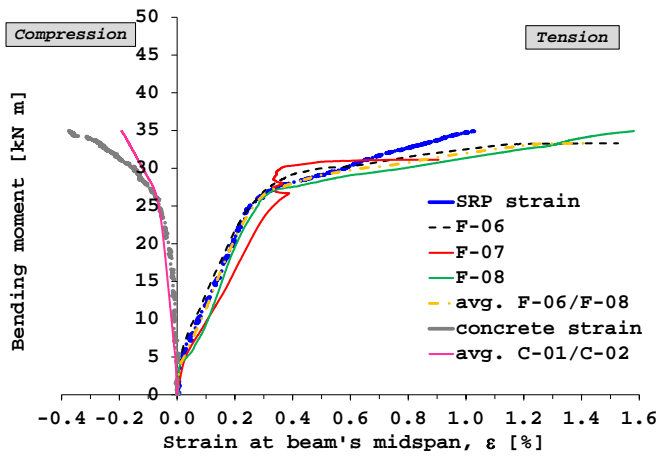
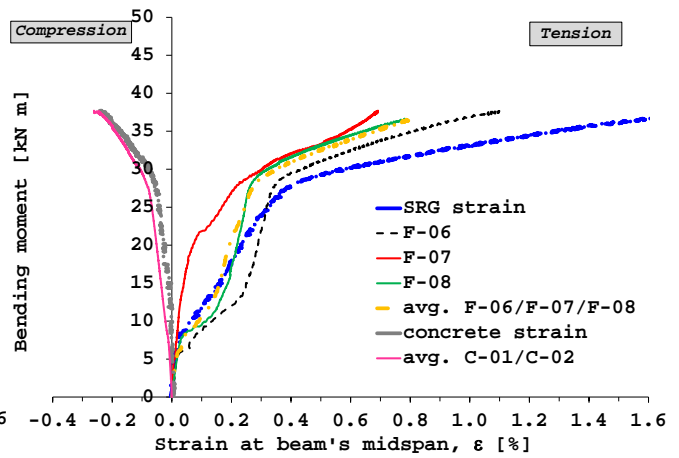


Figure 16 (only colour on the web)

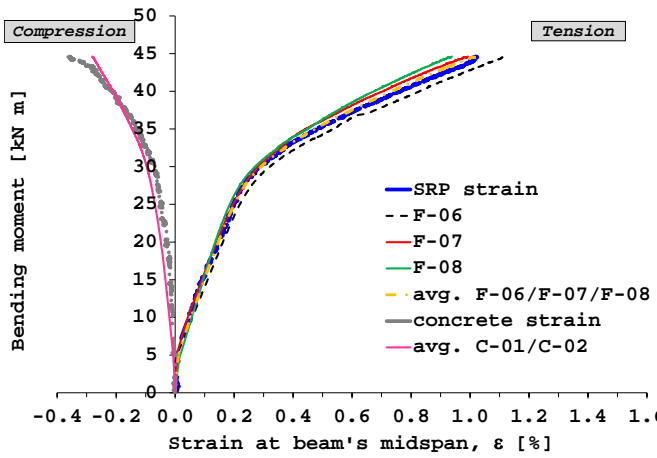
Test SRP-1LD



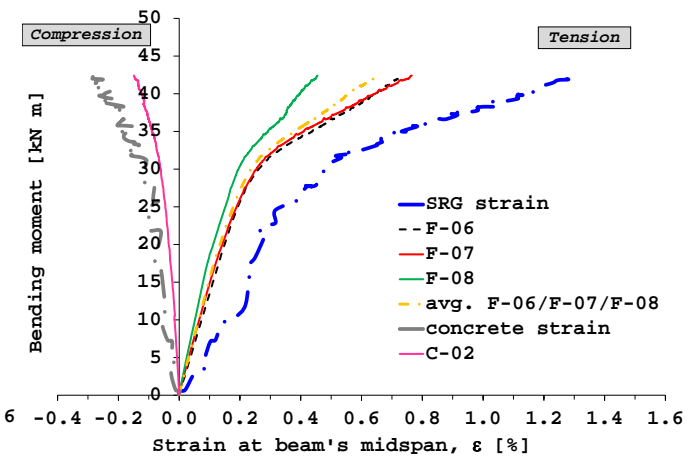
Test SRG-1LD



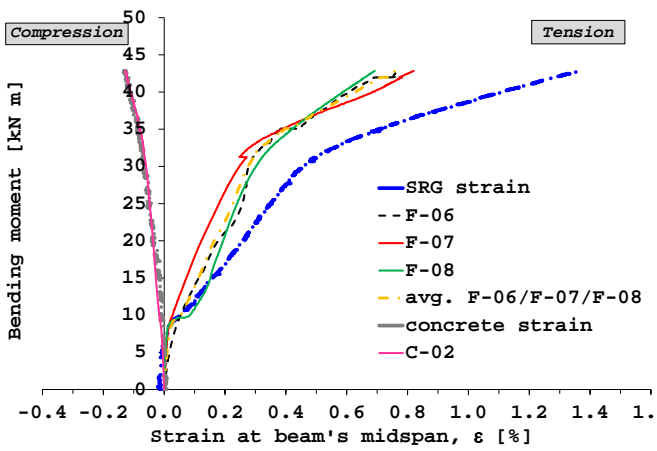
Test SRP-1MD



Test SRG-1MD



Test SRG-1MD-A



Test SRG-1MD-B

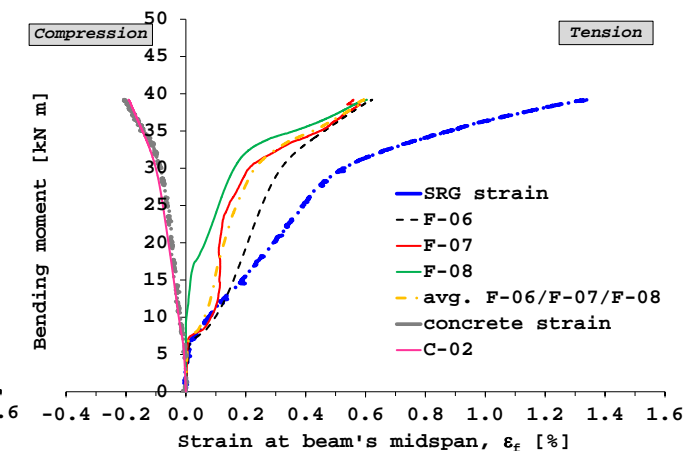
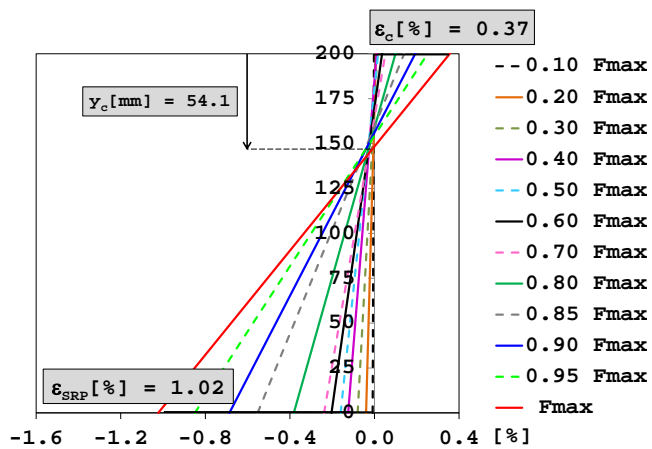
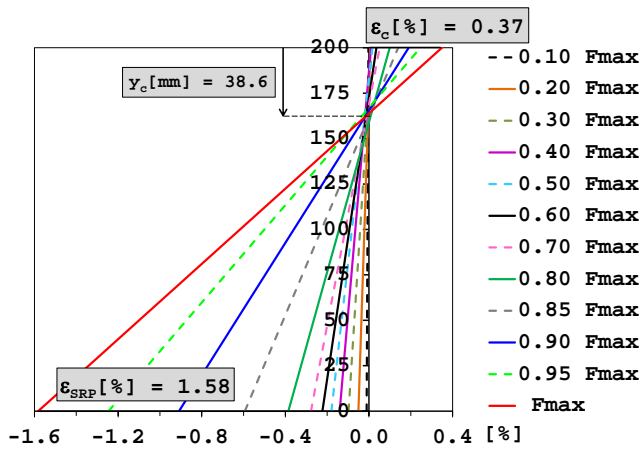


Figure 17 (only colour on the web)

Test SRP-1LD

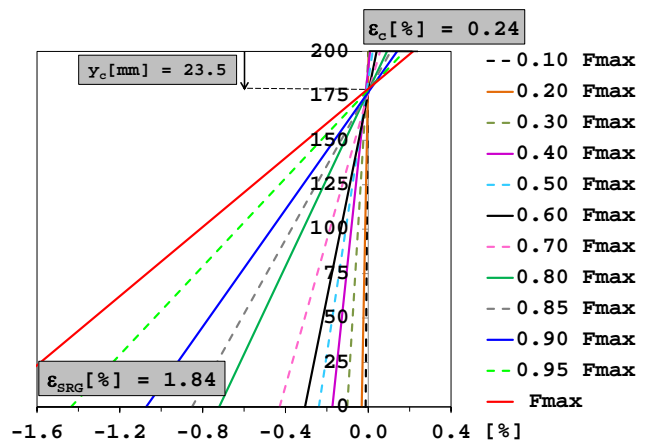


a)

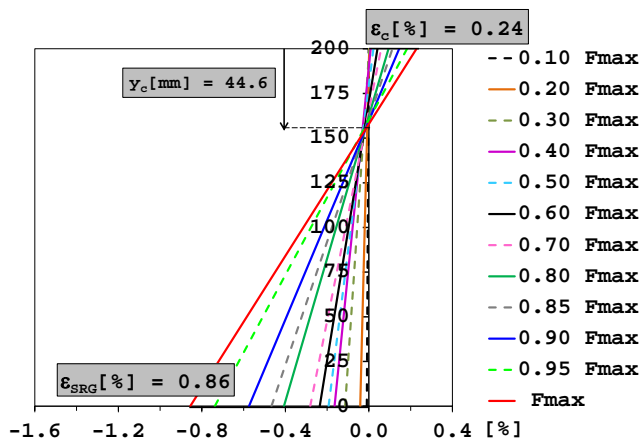


b)

Test SRG-1LD



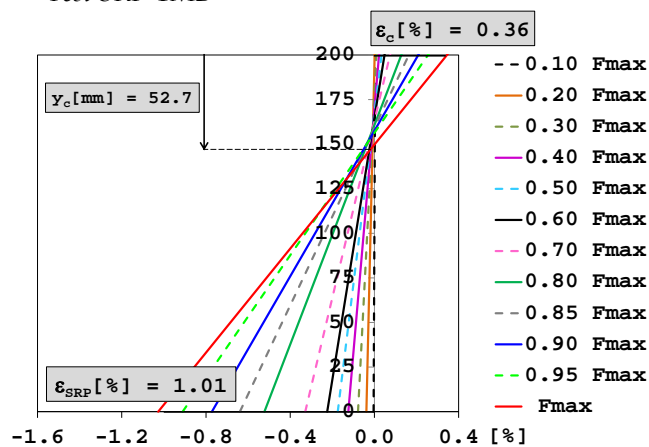
a)



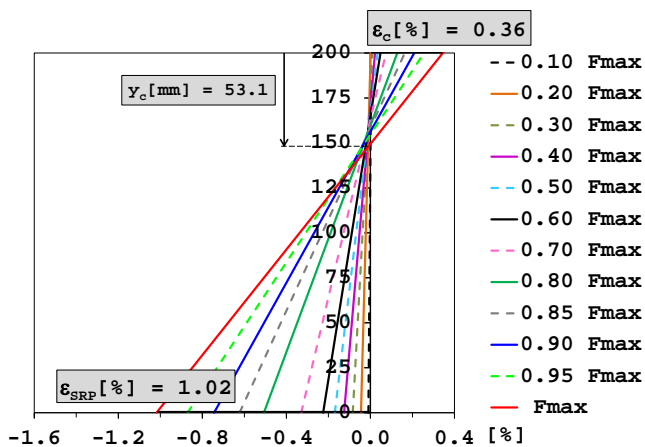
b)

Figure 18 (only colour on the web)

Test SRP-1MD

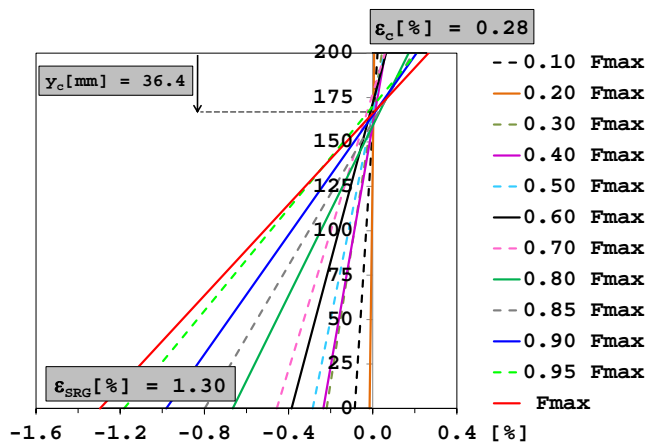


a)

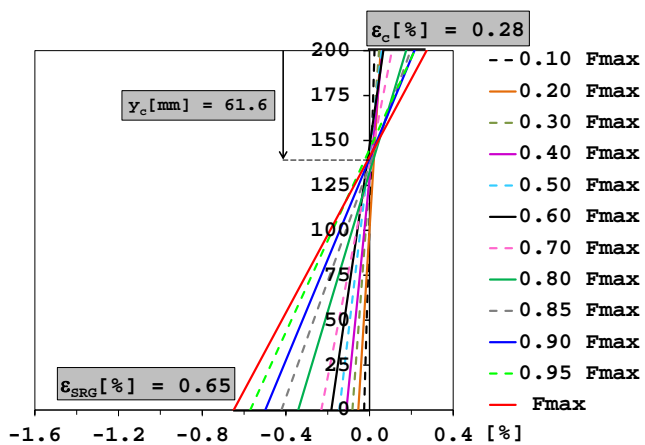


b)

Test SRG-1MD

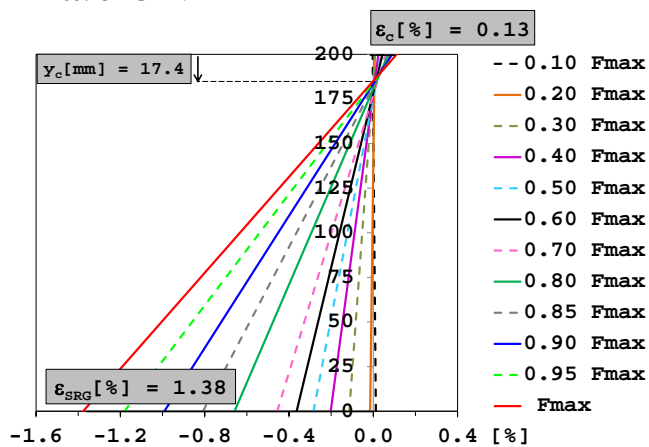


a)

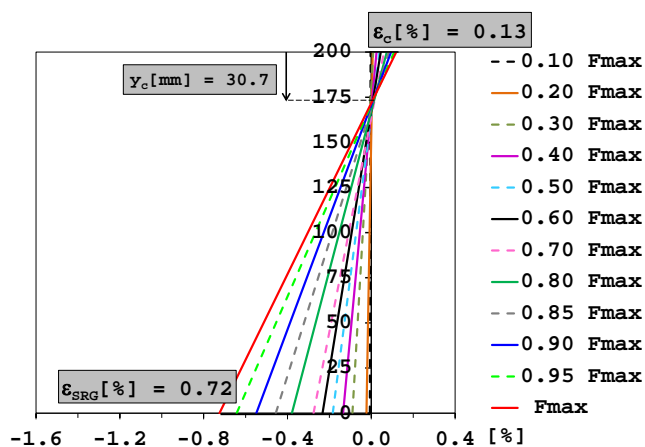


b)

Test SRG-1MD-A



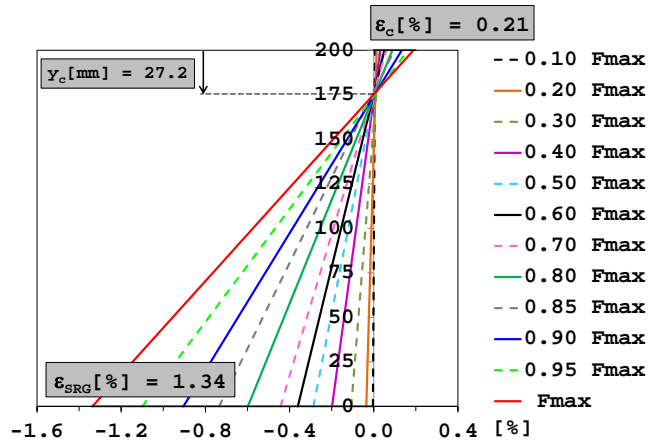
a)



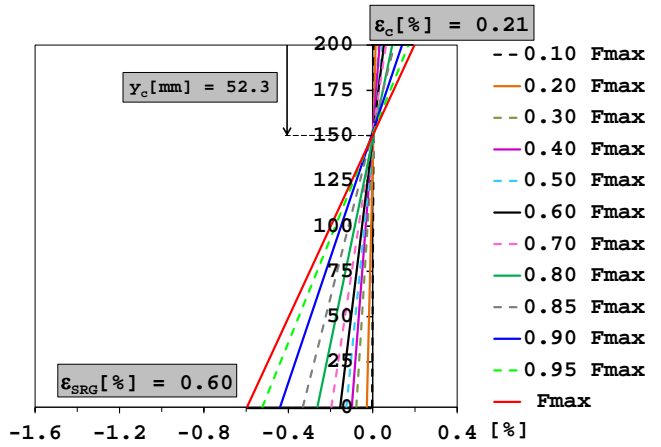
b)

Figure 18 (continued)

Test SRG-1MD-B

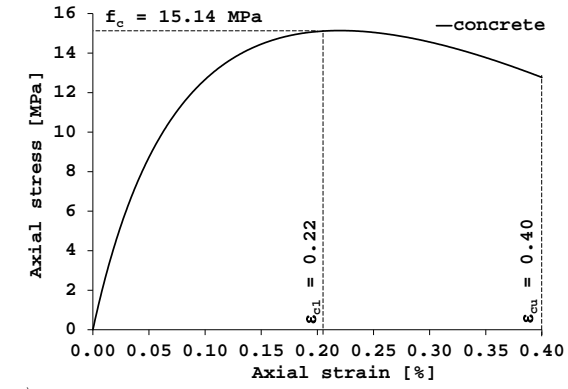


a)

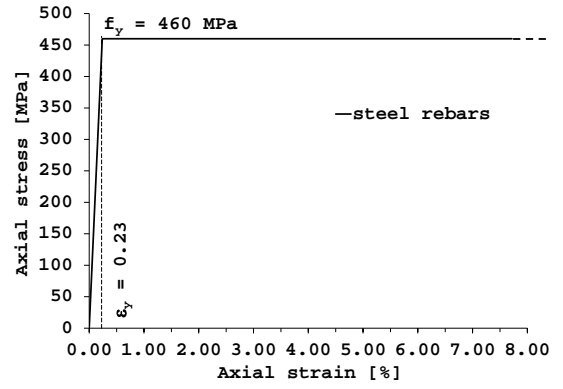


b)

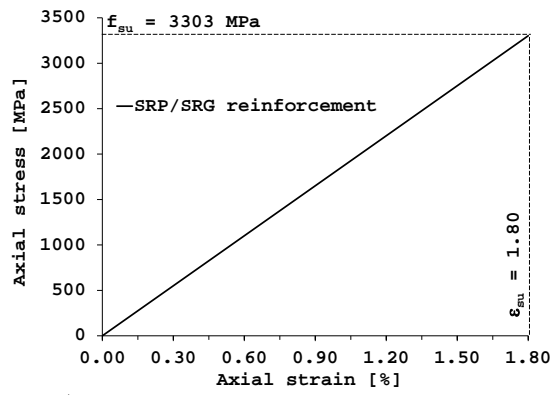
Figure 19



a)



b)



c)

Figure 20 (only colour on the web)

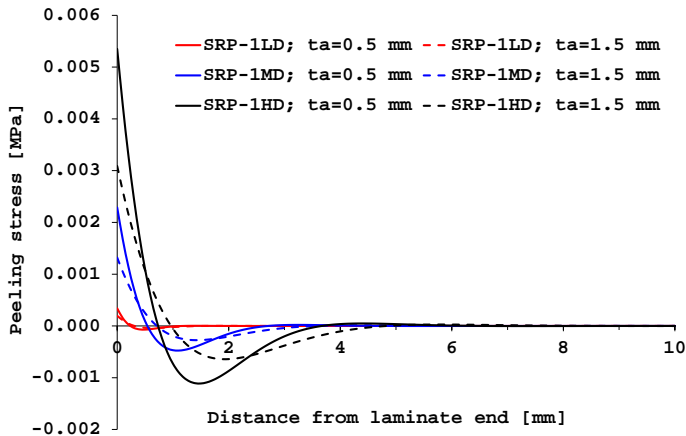
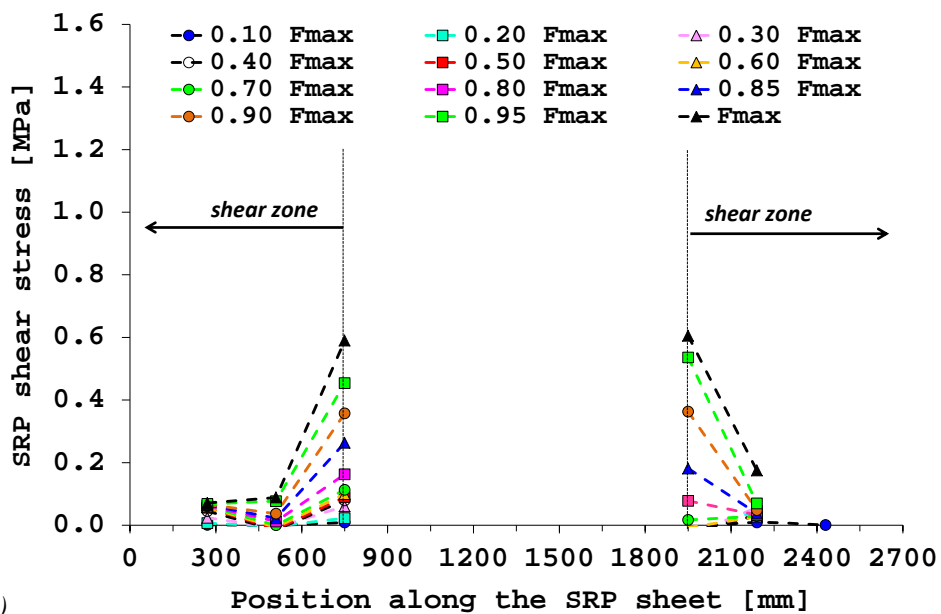
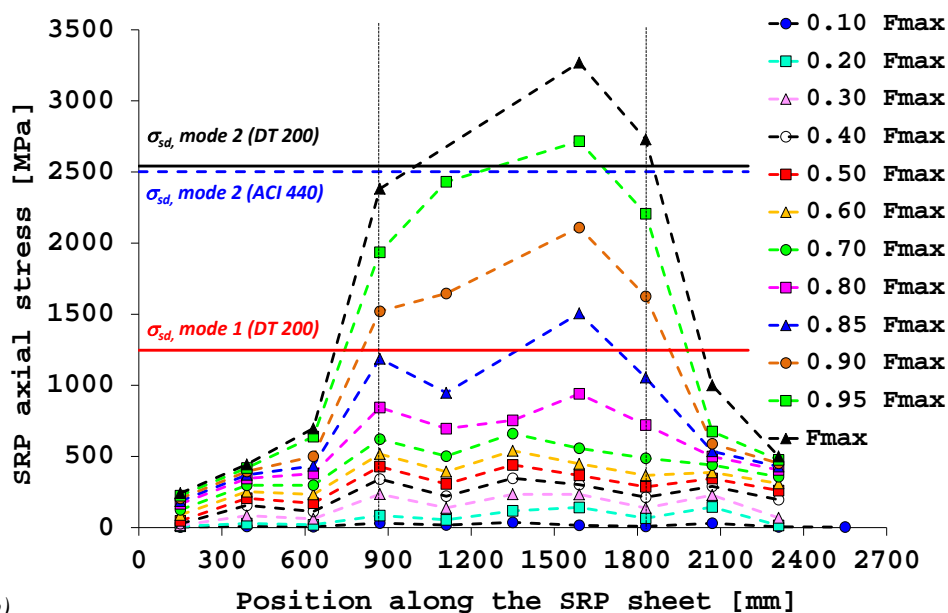


Figure 21 (only colour on the web)

Test SRP-1LD



a)



b)

Figure 22 (only colour on the web)

Test SRP-1MD

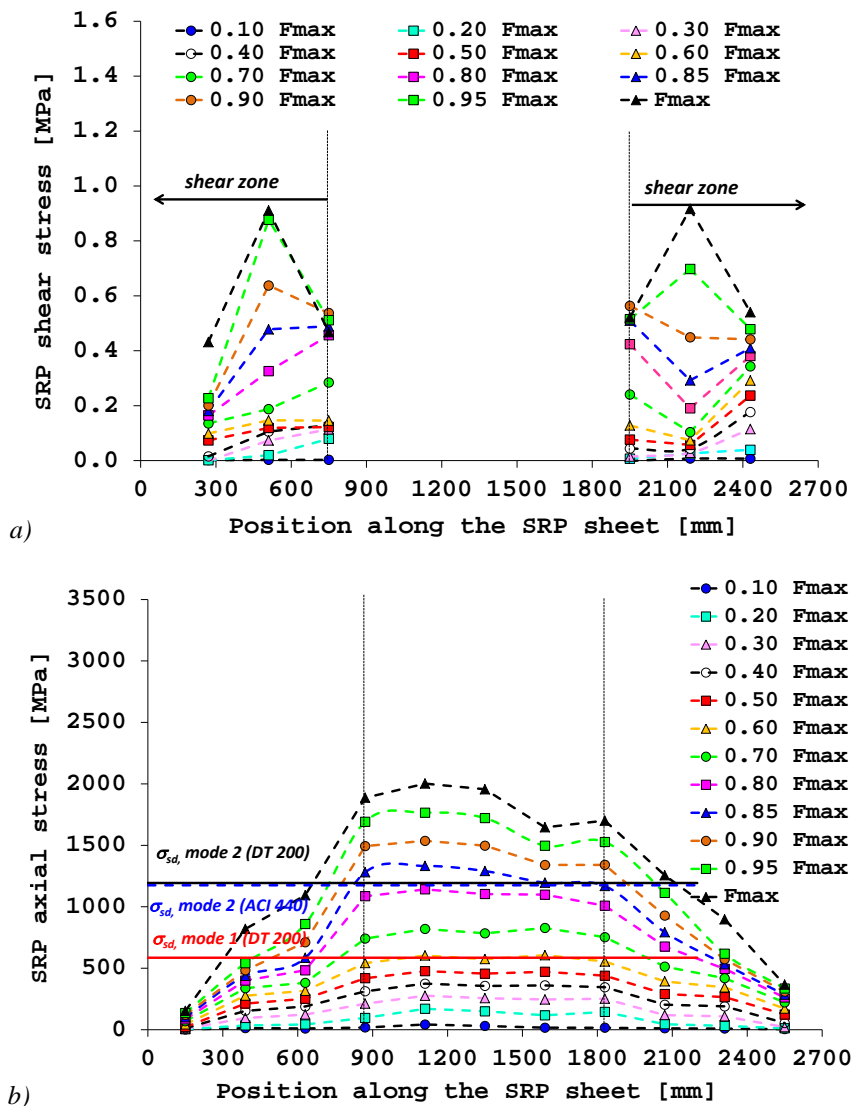
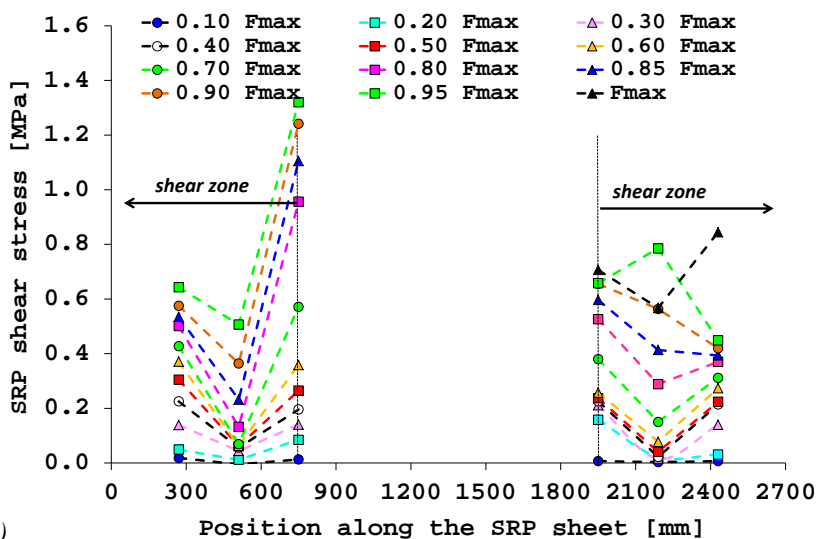
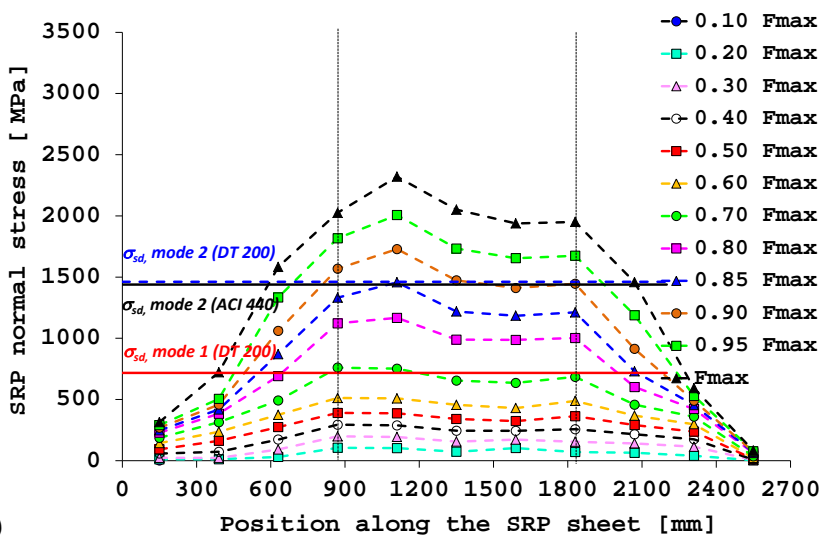


Figure 23 (only colour on the web)

Test SRP-1HD



a)



b)