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An effective learning strategy for cascaded object detection

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Abstract

To distinguish objects from non-objects in images in real-time, a suitable solution is to employ a cascade detector that consists of a sequence of node classifiers with increasing discriminative power. However, among the millions of image patches generated from an input image, only very few contain the searched object. When trained on these highly unbalanced data sets, the node classifiers tend to have poor performance on the minority class. Thus, we propose a learning strategy aimed at maximizing the node classifiers ranking capability rather than their accuracy. We also provide an efficient implementation yielding the same time complexity of the original Viola-Jones cascade training. Experimental results on highly unbalanced real problems show that our approach is both efficient and effective when compared to other node training strategies for skewed classes.

Keywords: pattern recognition, image processing, object detection, cascade, unbalanced data, ranking

1. Introduction

- Detecting objects in images and videos is a crucial task in many real-world
- ³ problems, ranging from face detection in images to pedestrian detection on

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roads, from biomedical image analysis to videosurveillance applications. From
the pattern recognition point of view, object detection can be cast as a classification problem in which one has to distinguish between the object class and
the "non-object" class. The difficulty is that the "non-object" class actually
contains all the patches in the images that are not instances of the searched
object and this makes very challenging this apparently simple problem.

First, whereas the object class is quite precisely defined, the non-object class 10 can be very inhomogeneous, since it includes several subclasses of other objects 11 very different each other. In real scenes, the searched objects are embedded in 12 a cluttered background containing various kinds of non-objects, some of which 13 are very different from what we are searching for, whereas others can be very 14 similar. As an example, when detecting faces in an office scene, it would be 15 simple to distinguish between a face and a chair, but it could be more complex 16 to distinguish between a face and a cartoon. 17

The second issue is that almost every real-world detection task requires processing a huge number of pixels and this could involve a computational load not easy to bear, specially if a complex classifier architecture is used.

The last point is related to the skewed class priors: in a typical detection problem, the vast majority of image locations do not contain the searched object and this makes detection a severely unbalanced classification problem. As a consequence, learning an effective classifier is very difficult since classifiers trained on highly unbalanced data sets tend to have poor performance on the minority class.

In this regard, a commonly adopted solution, originally proposed by Viola 27 and Jones [22], is to employ an ensemble of classifiers structured as a cascade 28 of dichotomizers with increasing complexity. Such an approach allows each di-29 chotomizer in the cascade to deal with only a part of the non-object class, thus 30 parting the complexity of the whole problem among the classifiers. In particular, 31 the first stages of the cascade are built to reject the most distinguishable back-32 ground regions, while the last stages are specialized to discriminate between 33 actual object and the most confusing background patches (see Fig. 1). This 34



Figure 1: Scheme of the cascade structure with N nodes

³⁵ aims at reducing the number of false positives produced by the detector and
³⁶ concentrate the computational complexity of the system on the last classifiers
³⁷ of the cascade.

Such approach is a valid solution to the first two issues. Indeed, whereas 38 a monolithic classifier would hardly ensure both a good sensitivity and a good 39 specificity and, in any case, typically requires an excessive computational bur-40 den, the cascade of dichotomizers provides a high constant sensitivity and a 41 growing specificity through the stages at a reasonable computational cost. This 42 is obtained by connecting classifiers that provide high sensitivity and sufficient 43 specificity on the subproblem they face and are sufficiently simple to ensure a 44 real-time response. To this end, a commonly used learning algorithm is Ad-45 aBoost [9] that allows both effective feature selection and proficient classifica-46 tion. 47

However, the original Viola-Jones approach does not deal well with the class 48 imbalance problem. In fact, even though each dichotomizer in the cascade is 49 trained to discriminate between the object class and a part of the non-object 50 class, the problem is asymmetric anyway since the object class is still much less 51 numerous. In this regard, AdaBoost is not able to effectively face the asymmetry 52 between the classes since it minimizes a quantity related to classification error, 53 that is significantly biased by skewed class priors. To address this problem, some 54 new approaches have been developed. In particular, Viola and Jones proposed 55

a new algorithm, AsymBoost [23], that handles the unbalanced classes through 56 an asymmetric weight updating mechanism of the samples in the training set. 57 Starting from this approach, Visentini et al. [24] proposed AsymBoost* that 58 extended the AsymBoost cascade algorithm by introducing a reactive control 59 of the asymmetry at both cascade and node learning level. Both these ap-60 proaches modify the learning strategy of the dichotomizer without abandoning 61 the beneficial AdaBoost scheme that simultaneously selects features and builds 62 the classifier. 63

Other approaches alter the Viola-Jones standard framework: for example, a 64 multiexit cascade is proposed in [13], where the *i*th node combines the scores 65 from the first i-1 dichotomizers, while [28] decouples the feature selection 66 process and the node classifier, which is designed to explicitly address the class 67 asymmetry. In [25] the two previous approaches are combined. All such solu-68 tions, however, do not guarantee that the benefits of the original cascade frame-69 work are still provided: in fact, the multiexit cascade increases the complexity 70 and the computational load of the single node whereas the separated feature 71 selection process could not make the optimal feature choice for the subsequent 72 classifier learning. 73

In this paper we address the problem of class imbalance within the Viola-74 Jones standard cascade framework where we introduce a new learning algorithm 75 for the node classifiers aimed at maximizing their ranking capability rather than 76 their accuracy. Although employed by all the techniques described before, accu-77 racy is not a correct measure for handling rare cases that have less impact than 78 common cases [27]. As a consequence, learning algorithms based on accuracy 79 lead to poor minority-class performance [26]. A common way to alleviate this 80 problem is to adopt a cost-sensitive learning method that assigns a higher cost 81 to the errors made on the minority class (as in AsymBoost and $AsymBoost^*$). 82 The difficulty of this approach lies in correctly defining the cost matrix: a com-83 mon choice is to set the ratio of the error costs equal to the ratio of the prior 84 probabilities of the two classes, but it is not always possible to reliably estimate 85 such value. Another possible approach is to attempt to balance the class distri-86

⁸⁷ butions by undersampling the majority class or by oversampling the minority class, but both solutions present serious drawbacks. Whereas undersampling can potentially remove important examples of the majority class, the samples artificially generated and added to the minority class in oversampling can produce an unfaithful training set [12].

Our approach is to use rank metrics instead of accuracy metrics for train-92 ing the single dichotomizer in the cascade. More specifically, rank metrics are 93 more concerned with the relative ordering of cases than with making absolute 94 predictions for cases and thus place more emphasis on learning to distinguish 95 classes than on learning the internal structure of classes [3]. To this end, the 96 training of the node dichotomizers is based on a reformulation of *RankBoost* for 97 bipartite ranking problems [8], suitably modified to be embedded in a cascade 98 structure. This solution allows the detector to take advantage of the benefits 99 of the standard cascade framework and to effectively face the asymmetry still 100 present in each node classifier training. A partial and preliminary presentation 101 of this approach has been made in [2], whereas in this paper we extend the theo-102 retical framework and consider other significant detection problems in the exper-103 iments. In particular, the cascade trained with rank-based node dichotomizers 104 is compared with the original Viola-Jones method, with AsymBoost and with 105 AsymBoost^{*}. Moreover, we have also considered a cascade of dichotomizers 106 trained with *RUSBoost* [18], a boosting-based learning algorithm that faces the 107 class imbalance by undersampling the majority class. As real-world applica-108 tions, we have examined in our experiments a face detection problem and two 109 medical imaging problems: the detection of microcalcifications on digital mam-110 mograms (to extend the preliminary comparison in [2]) and the detection of 111 microaneurysms in digital fundus images. All the examined applications are 112 characterized by a considerable class imbalance and the obtained results show 113 that the proposed approach provides performance similar or better than the 114 other algorithms thus confirming its effectiveness. 115

The rest of this paper is organized as follows: Section 2 recalls some previously proposed learning strategies for the node classifier, while in Section 3 we ¹¹⁸ describe the rank-based learning algorithm for the node dichotomizer. Section 4
¹¹⁹ provides an efficient implementation of the proposed approach. In Section 5 the
¹²⁰ results of an extensive experimental comparison are reported and discussed.
¹²¹ Finally, Section 6 draws some conclusions and outlines directions for future
¹²² research.

¹²³ 2. Accuracy-based node learning strategies for skewed classes

To point out the drawbacks of accuracy-based node training in the original 124 Viola-Jones framework, let us briefly recall the AdaBoost approach. A weak 125 learner $h_{\tau}(\cdot)$ is selected in each of a series of rounds $\tau = 1, 2, \ldots$, so as to 126 minimize the weighted exponential loss $\sum_{j} D_{\tau}(j) \exp(-y_{j}h_{\tau}(\mathbf{x}_{j}))$, where $D_{\tau}(j)$ 127 is the weight on the *j*th sample \mathbf{x}_j and $y_j \in \{-1, 1\}$ is the class label of \mathbf{x}_j . It is 128 easy to see that, in the case of highly skewed classes, such sum is dominated by 129 the error produced on the majority class and thus the choice of the weak learner 130 is not optimal for predicting the minority class. The approaches proposed so far 131 to alleviate such problem can be attributed to two different groups: cost-based 132 strategies and sampling-based strategies. 133

134 2.1. Cost-based strategies

This category includes the methods that employ the Adaboost learning pro-135 cedure, with a cost assigned to false negatives greater than to false positives. 136 Both AsymBoost and AsymBoost* follow this way. In AsymBoost, each sample 137 \mathbf{x}_j is pre-weighted at each round with an asymmetric cost exp $\left(\frac{1}{T}y_j\log\sqrt{k}\right)$ 138 where T is the total number of rounds of the dichotomizer. The parameter k139 estimates how much more false negatives cost than false positives and its choice 140 should bias the classifier to perform well on the minority object class. The dif-141 ference between AsymBoost and $AsymBoost^*$ is in the value of k that is fixed 142 in AsymBoost whereas it is automatically tuned at each round in AsymBoost^{*}. 143 Other cost-sensitive boosting algorithms have been proposed in the literature 144 [11, 7, 21, 19]. The problem common to all these methods is that specific cost 145 information is rarely available or hard to estimate, as well as the ratio between 146 147 the costs.

148 2.2. Sampling-based strategies

Another popular solution is to modify the original distribution of the data so 149 as to obtain an artificially balanced training set. This approach can be accom-150 plished by two means: undersampling the majority class by eliminating data 151 points until it reaches the size of the minority class or oversampling the minor-152 ity class by adding artificially generated data points until the desired balance 153 is achieved. An algorithm introducing data undersampling into the AdaBoost 154 procedure is *RUSBoost* [18] that applies a random undersampling of the major-155 ity class for building a balanced training set at each iteration of the boosting 156 algorithm. On the other hand, SMOTEBoost [5] applies oversampling to Ad-157 aBoost according to SMOTE [4], an algorithm that oversamples the minority 158 class by introducing new, non-replicated minority-class examples. Even though 159 very popular, such approach is hardly applicable when dealing with high dimen-160 sional feature spaces, as in the case of the Viola-Jones framework. Moreover, in 161 particular applications (e.g. medical imaging) it could be unsafe to add artifi-162 cially generated samples that do not correspond to real situations. 163

¹⁶⁴ 3. Ranking-based node learning

In this section we draw a ranking-based learning strategy to train the cascade dichotomizers. The dichotomizer $H_i(\mathbf{x})$ added at the *i*th stage is based on a reformulation of *RankBoost* for bipartite ranking problems [8], suitably modified to be embedded in a cascade structure. It consists of a linear combination of weak learners $h_{i,\tau}(\mathbf{x}) \in \{0,1\}$ (0 for the negative class, 1 for the positive one) weighted by $\alpha_{i,\tau} \in \mathbb{R}$ and added in subsequent rounds $\tau = 1, 2, \ldots$ so that after *t* rounds we obtain

$$H_{i,t}(\mathbf{x}) = \sum_{\tau=1}^{t} \alpha_{i,\tau} h_{i,\tau}(\mathbf{x}).$$
(1)

To simplify the notation, let us omit the subscript *i* throughout this section. A weak learner $h_{\tau}(\mathbf{x})$ consists of a simple *decision stump* given by

$$h_{\tau}(\mathbf{x}) = \begin{cases} 1 & \text{if } \varphi_{\tau}(\mathbf{x}) > \theta_{\tau} \\ 0 & \text{if } \varphi_{\tau}(\mathbf{x}) \le \theta_{\tau} \end{cases}$$
(2)

where $\varphi_{\tau}(\mathbf{x}) \in \mathcal{F}$ is the feature selected at round τ from the feature set \mathcal{F} and θ_{τ} is the threshold selected at round τ in the range $\left(\min_{\mathbf{x}\in\mathcal{T}}\varphi_{\tau}(\mathbf{x}), \max_{\mathbf{x}\in\mathcal{T}}\varphi_{\tau}(\mathbf{x})\right)$, with \mathcal{T} being the training set. Differently from the original *RankBoost*, such weak learners do not abstain and are $\{0, 1\}$ -valued so as to preserve the ordering information provided by the feature while ignoring its specific scoring information.

To maximize the ranking capability of the dichotomizer, let us consider the crucial pairs (\mathbf{p}, \mathbf{n}), defined as all the sample pairs made by a positive sample \mathbf{p} and a negative sample \mathbf{n} . A crucial pair is correctly ranked when $H_t(\mathbf{n}) < H_t(\mathbf{p})$. Therefore, our goal is to minimize the ranking loss R_t , defined as the number of misranked crucial pairs and given by¹

$$R_t = \sum_{(\mathbf{p},\mathbf{n})} [H_t(\mathbf{n}) \ge H_t(\mathbf{p})]$$
(3)

¹⁸⁵ A weight distribution $w_t(\mathbf{p}, \mathbf{n})$ is maintained over the crucial pairs so that the ¹⁸⁶ misranked crucial pairs will be more influential in the following rounds. The ¹⁸⁷ weight update rule is given by

$$w_{t+1}(\mathbf{p}, \mathbf{n}) = \frac{w_t(\mathbf{p}, \mathbf{n}) \exp\left(\alpha_t \left(h_t(\mathbf{n}) - h_t(\mathbf{p})\right)\right)}{W_t}$$
(4)

where W_t is a normalization factor so that $\sum_{\mathbf{p},\mathbf{n}} w_{t+1}(\mathbf{p},\mathbf{n}) = 1$. Assuming $\alpha_t > 0$, the update rule decreases the weight of crucial pairs in case of correct ranking (i.e., $h_t(\mathbf{p}) = 1$ and $h_t(\mathbf{n}) = 0$) and increases the weight otherwise. Combining Eq. 3 with Eq. 4, the goal becomes to minimize the weighted number

¹the notation [pr] (Iverson bracket) is defined to be 1 if predicate pr holds and 0 otherwise.

¹⁹² of misranked crucial pairs R_t^w (weighted ranking loss) given by

$$R_t^w = \sum_{(\mathbf{p},\mathbf{n})} w_t(\mathbf{p},\mathbf{n}) [H_t(\mathbf{n}) \ge H_t(\mathbf{p})]$$
(5)

from which $h_t(\cdot)$ (i.e., $\varphi_t(\cdot)$ and θ_t) and α_t can be chosen by

$$(h_t, \alpha_t) = \operatorname*{arg\,min}_{h,\alpha} \sum_{(\mathbf{p}, \mathbf{n})} w_t(\mathbf{p}, \mathbf{n}) [H_{t-1}(\mathbf{n}) + \alpha h(\mathbf{n}) \ge H_{t-1}(\mathbf{p}) + \alpha h(\mathbf{p})] \quad (6)$$

¹⁹⁴ In fact, α_t can be found directly by minimizing an upperbound of R_t^w as in [8], ¹⁹⁵ which yields

$$R_t^w \le \sqrt{1 - r_t^2} \tag{7}$$

196 by choosing

$$\alpha_{h_t} = \frac{1}{2} \ln \left(\frac{1 + r_t}{1 - r_t} \right) \tag{8}$$

197 where

$$r_t = \sum_{\mathbf{p},\mathbf{n}} w_t(\mathbf{p},\mathbf{n})(h_t(\mathbf{p}) - h_t(\mathbf{n}))$$
(9)

¹⁹⁸ Then, combining Eq. 6 with Eq. 7, the choice of $h_t(\cdot)$ at round t becomes

$$h_t = \arg\max_h |r_t| \tag{10}$$

In summary, at each round t, the choice of the weak learner $h_t(\cdot)$ and subsequently the selection of the feature $\varphi_t(\cdot)$ is made to maximize the correct pairwise ranking. An example of the training process described so far is shown in Fig. 2.

203 4. Efficient implementation of ranking-based training

The training procedure presented in the previous section is embedded in a Viola-Jones standard cascade structure which is constructed as follows. Let \mathcal{P} and \mathcal{N} denote the sets of positive and negative samples. The node classifiers $H_i(\mathbf{x})$ are added in subsequent stages i = 1, 2, ... until the desired false positive rate F_{target} is reached or $\mathcal{N} = \{\emptyset\}$. To construct the *i*th node classifier $H_i(\mathbf{x})$, \mathcal{P} and \mathcal{N} (hereafter referred to as *pool*) are used to form a training set \mathcal{T}_i and



Figure 2: An example of the training process for a node classifier. At each round t (t = 3 in the depicted graph), a new weak learner which is restricted to use a single feature is added. The resulting classifier function is then used to rank the samples in the node training set. The sum of weights of misranked crucial pairs (highlighted with a gray box) is evaluated and the feature minimizing this quantity is selected and added to the current node.

²¹⁰ a validation set \mathcal{V}_i , respectively to train and to set the decision threshold Θ_i of ²¹¹ the *i*th node classifier $H_i(\mathbf{x})$ so as to meet the node learning goals d (detection ²¹² rate) and f (false positive rate) (see Algorithm 1, lines 13-14).

A naive implementation of this approach may result in a computational 213 workload not easy to sustain in the training phase, especially when dealing with 214 millions of negative samples, as in the case of many object detection problems. 215 Indeed, there are three major issues that make it challenging to efficiently im-216 plement the proposed learning strategy: (i) the high computational complexity 217 of weak learner selection in Eq. 10; (ii) the computation of features throughout 218 training; and (iii) the need of a criterion to control the number of training rounds 219 in a node. Each of these problems is discussed in the following subsections. The 220 pseudocode of the overall training procedure is provided in Algorithm 1 along 221 with the list of used symbols. 222

223 4.1. Reducing the time complexity of weak learner selection

From Eq. 10, the time-per-round requirements are $O(|\mathcal{T}_i^{\mathbf{p}}| \cdot |\mathcal{T}_i^{\mathbf{n}}| \cdot |\mathcal{H}|)$, where $\mathcal{T}_i^{\mathbf{p}}$ is the subset of \mathcal{T}_i containing only positive samples \mathbf{p} , $\mathcal{T}_i^{\mathbf{n}}$ is the subset of \mathcal{T}_i containing only negative samples \mathbf{n} and \mathcal{H} is the set of candidate weak learners $h(\cdot)$. To improve this, as suggested in [8] we maintain only a one-argument weight distribution $v_{i,t}(\mathbf{x})$ under the constraint

$$w_{i,t}(\mathbf{p}, \mathbf{n}) = v_{i,t}(\mathbf{p})v_{i,t}(\mathbf{n}) \tag{11}$$

Then, omitting i, t subscripts we obtain from Eq. 9

$$r = \sum_{\mathbf{p},\mathbf{n}} w(\mathbf{p},\mathbf{n}) \left(h(\mathbf{p}) - h(\mathbf{n}) \right)$$

$$= \sum_{\mathbf{p}} \sum_{\mathbf{n}} v(\mathbf{p}) v(\mathbf{n}) \left(h(\mathbf{p}) s(\mathbf{p}) + h(\mathbf{n}) s(\mathbf{n}) \right)$$

$$= \sum_{\mathbf{p}} \left(v(\mathbf{p}) \sum_{\mathbf{n}} v(\mathbf{n}) \right) h(\mathbf{p}) s(\mathbf{p}) + \sum_{\mathbf{n}} \left(v(\mathbf{n}) \sum_{\mathbf{p}} v(\mathbf{p}) \right) h(\mathbf{n}) s(\mathbf{n})$$

$$= \sum_{\mathbf{x}} \pi(\mathbf{x}) h(\mathbf{x})$$
(12)

230 where

$$s(\mathbf{x}) = \begin{cases} +1, & \text{if } \mathbf{x} \in \mathcal{T}_i^{\mathbf{p}} \\ -1, & \text{if } \mathbf{x} \in \mathcal{T}_i^{\mathbf{n}} \end{cases}$$
(13)

231 and

$$\pi(\mathbf{x}) = s(\mathbf{x})v(\mathbf{x}) \sum_{\mathbf{x}':s(\mathbf{x})\neq s(\mathbf{x}')} v(\mathbf{x}')$$
(14)

is referred to as the *potential* $\pi(\mathbf{x})$ and can be precomputed at the beginning of each round in only $O(|\mathcal{T}_i^{\mathbf{p}}| + |\mathcal{T}_i^{\mathbf{n}}|) = O(|\mathcal{T}_i|)$ time. Combining Eqs. 2, 10 and 12 we obtain the final solution

$$h_{i,t} = \arg\max_{h} \left| \sum_{\mathbf{x}:\varphi(\mathbf{x}) > \theta} \pi_{i,t}(\mathbf{x}) h(\mathbf{x}) \right|$$
(15)

which has the reduced time complexity $O(|\mathcal{T}_i| \cdot |\mathcal{H}|)$. Remarkably, this is the same time complexity of the weak learner selection in the Viola-Jones standard cascade framework.

238 4.2. On-line efficient features computation

From Eq. 2, it follows that each candidate weak learner $h(\mathbf{x}) \in \mathcal{H}$ relies on the evaluation of a feature $\varphi(\mathbf{x}) \in \mathcal{F}$ on a sample \mathbf{x} with respect to a

Algorithm 1 Ranking-based cascade training

$ \begin{array}{c} F_{t,i} \\ f, . \\ d: \\ \mathcal{P}, \\ \mathcal{T}_{i}, \\ \mathcal{T}_{i} \\ v_{i}, \\ v_{i}, \\ v_{i}, \\ \varphi(: \\ H_{i} \\ \Theta_{i} \\ h_{i}, \\ \alpha_{i}, \end{array} $	$\begin{array}{llllllllllllllllllllllllllllllllllll$		
1: 1	$i \leftarrow 0; F \leftarrow 1.0;$ while $E > E \qquad \land N \neq [\emptyset]$ do	/* .]]]. */	
2:	while $F > F_{target} \land N \neq \{\emptyset\}$ do	/ add a new node /	
3: 4.	$i \leftarrow i + 1, i \leftarrow 0, j_{i,0} \leftarrow 1.0$	$(\cdot) \in \mathcal{H} \text{ on } \mathcal{T}$	
4. 5.	$v_{1,0}(\mathbf{n}) = 1/ \mathcal{T}^{\mathbf{p}} $; $v_{1,0}(\mathbf{n}) = 1/ \mathcal{T}^{\mathbf{n}} $	$() \subset \mathcal{H}$ on \mathcal{J}_i	
6.	while $f_{i,i} > f \land \neg varston do$	/* add a new weak learner */	
7:	$t \leftarrow t+1$		
8:	$\pi_{i,t}(\mathbf{x}) = s(\mathbf{x})v_{i,t}(\mathbf{x})\sum_{\mathbf{x}' \in \mathcal{S}(\mathbf{x}) \setminus \mathcal{S}(\mathbf{x}')} v_{i,t}(\mathbf{x})$	x') /* precompute potentials */	
9:	$h_{i,t} = \arg \max_{k} r_{i,t} $	/* find best weak learner */	
	$\alpha_{i,t} = \frac{1}{2} \ln \left(\frac{1+r_{i,t}}{1-r_{i,t}} \right) \Big _{h=h_{i,t}}$ where $r_{i,t} = \sum_{\mathbf{x}:\varphi(\mathbf{x})>\theta} \pi_{i,t}(\mathbf{x})h(\mathbf{x})$		
10: 11:	$v_{i,t+1}(\mathbf{x}) _{\mathbf{x}=\mathbf{p},\mathbf{n}} = \frac{v_{i,t}(\mathbf{x})e^{-s(\mathbf{x})\alpha_{i,t}h_{i,t}(\mathbf{x})}}{\sum_{\mathbf{x}}v_{i,t}(\mathbf{x})e^{-s(\mathbf{x})\alpha_{i,t}h_{i,t}(\mathbf{x})}}$ precompute weak learner $h_{i,t}$ on \mathcal{V}_i and	$\frac{1}{2}$ /* sample weights update */ d ${\cal N}$	
12:	$H_{i,t}(\mathbf{x}) _{\mathbf{x}\in\mathcal{V}_i} = \sum_{\tau=1}^t \alpha_{i,\tau} h_{i,\tau}(\mathbf{x})$	/* evaluate $H_{i,t}(\cdot)$ on \mathcal{V}_i */	
13:	$\Theta_i: \{\mathbf{p} \in \mathcal{V}_i : H_{i,t}(\mathbf{p}) \ge \Theta_i\} \ge d \mathcal{V}_i^{\mathbf{p}} $	/* meet node learning goal d */	
14:	$f_{i,t} \leftarrow f_{i,t-1} \left \{ \mathbf{n} \in \mathcal{V}_i : H_{i,t}(\mathbf{n}) \ge \Theta_i \} \right $	/* update false positive rate $f_{i,t}$ */	
15:	$varstop \leftarrow [Var\left(\{f_{i,\tau}\}_{\tau=t-\Delta,\dots,t}\right) \le \epsilon]$	/* stop criterion $*/$	
16:	end while		
17:	output $H_i(\mathbf{x}) = \left \sum_{\tau=1}^t \alpha_{i,\tau} h_{i,\tau}(\mathbf{x}) \ge \Theta_i \right $	/* the final $i{\rm th}$ node classifier */	
18:	$F \leftarrow F \times f_{i,t}$	update overall false positive rate $*/$	
19:	if $F > F_{target}$ then /* prepar	we \mathcal{T}_{i+1} and \mathcal{V}_{i+1} for a new node */	
20:	$\mathcal{T}_{i+1} = \mathcal{T}_i \setminus \{\mathbf{n} \in \mathcal{T}_i : H_i(\mathbf{n}) = 0\} ; \mathcal{V}_{i+1}$	$= \mathcal{V}_i \setminus \{\mathbf{n} \in \mathcal{V}_i : H_i(\mathbf{n}) = 0\}$	
21:	$\mathcal{N} = \{\mathbf{n} \in \mathcal{N} : H_i(\mathbf{n}) = 1\}$		
22:	refill adequately both \mathcal{T}_{i+1} and \mathcal{V}_{i+1} by	y random sampling from \mathcal{N}	
23:	end if		
24:	end while		

threshold θ . Being O(1) the per-feature evaluation time requirement [22], pre-241 calculating the features for all the samples used in the training phase would 242 cost $O(|\mathcal{F}|(|\mathcal{P}| + |\mathcal{N}|))$. Moreover, additional costs have to be considered when 243 there is no available system memory to keep all these feature values at the same 244 time, and a caching strategy is used instead. To cope with these problems, we 245 draw an *on-line* features computation strategy aimed at minimizing the num-246 ber of needed features calculations and keeping feature values into memory until 247 they are no longer needed. In fact, only three contributions are required to train 248 the *i*th node: (i) $|\mathcal{T}_i| |\mathcal{F}|$ feature values for finding the best weak learner on \mathcal{T}_i 249 (see Algorithm 1, line 9); (ii) $t |\mathcal{V}_i|$ feature values for evaluating the node clas-250 sifier $H_{i,t}(\mathbf{x})$ on \mathcal{V}_i (see Algorithm 1, lines 12 and 20); and (iii) $t |\mathcal{N}|$ feature 251 values for evaluating the *i*th node classifier on \mathcal{N} (see Algorithm 1, line 21). 252 Therefore, we can pre-compute and keep into memory the $|\mathcal{T}_i| |\mathcal{F}|$ feature values 253 before training the *i*th node (see Algorithm 1, line 4) and do the same for each 254 selected feature evaluated on \mathcal{V}_i and \mathcal{N} at each round (see Algorithm 1, line 11). 255 When a node has been trained, we release the memory used for storing the fea-256 ture values calculated on the samples discarded from $\mathcal{T}_i, \mathcal{V}_i$ and \mathcal{N} . In this way, 257 the time-per-node requirements for feature computation are only $O(|\mathcal{T}_i||\mathcal{F}|)$, 258 where we supposed $t(|\mathcal{V}_i| + |\mathcal{N}|) \ll |\mathcal{T}_i| |\mathcal{F}|$ since $|\mathcal{N}|$ decreases exponentially 250 throughout the cascade (see Algorithm 1, lines 21-22) and t can be supposed to 260 be a relatively small number (as it will be discussed in the next paragraph). 261

262 4.3. Determining the number of training rounds

In principle, the training rounds for the *i*th node go on until the node learn-263 ing goals d and f are met. In fact, the decision threshold Θ_i of the *i*th node 264 classifier $H_i(\mathbf{x})$ is always chosen at each round so as to meet d, hence the number 265 of rounds is governed only by whether the condition $f_{i,t} \leq f$ is satisfied, being 266 $f_{i,t}$ the actual false positive rate of the *i*th node achieved at round *t*. How-267 ever, when the classification task is getting more and more complex throughout 268 the cascade, it could be too difficult to satisfy such a condition, thus causing 269 several unnecessary features to be added without substantially reducing $f_{i,t}$. 270

To solve this problem, we add new features until a significant reduction of $f_{i,t}$ can be achieved. Let $\psi_i(\Delta) = \{f_{i,\tau}\}_{\tau=t-\Delta,t-\Delta+1,...,t}$ be the latest Δ achieved false positive rates of the *i*th node. Then, we define a stopping criterion being *varstop* = $[Var(\psi_i(\Delta)) \leq \epsilon]$ so that new features are added until the condition $f_{i,t} > f \land \neg varstop$ holds (see Algorithm 1, lines 6,15).

276 5. Experiments

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To evaluate the performance of the proposed approach, we have considered 277 three different real problems with highly unbalanced classes. The first is face de-278 tection that represents a well-known topic in scientific literature and a historical 279 problem for the cascade approach as it was used in the seminal paper of Viola 280 and Jones [22]. The other two problems belong to the field of medical image 281 analysis. In particular, we examined the detection of microcalcifications (MC) 282 on digital mammograms for the automated early detection of breast cancer, and 283 the detection of microaneurysms (MA) on digital ocular fundus images, that is 284 an important task in computer aided diagnosis of diabetic retinopathy. 285

In all the experiments, Haar-like features were used to describe the regions to be detected. These features are simple and computationally efficient and have been successfully used in face detection and classification problems. As in [10], we considered the set of (i) edge features; (ii) line features; (iii) center-surround features; (iv) and special diagonal line features. All features have been scaled and separately translated across all possible combinations on the subwindow, thus obtaining tens of thousands of features.

To verify the effectiveness of our approach (hereafter referred to as *RankingCascade*) we also analyzed the behavior of other methods proposed in the literature. In particular, we implemented and evaluated the performance of different cascades that represent different solutions for facing class imbalance:

• AsymBoost-based Cascade (hereafter abbreviated as Asym). AsymBoost [23] is a cost-sensitive variant of AdaBoost that uses a parameter k to estimate the balance between the errors on the positive (False Negative Rate, FNR) and the negative class (False Positive Rate, FPR). The value of k is usually chosen equal to the imbalance level, i.e., the ratio between the cardinality of the negative and the positive sets.

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• $AsymBoost^*$ (hereafter abbreviated as $Asym^*$). This method, proposed in [24], is a variant of Asym and introduces two principal changes: a dynamic optimization of the FPR in each stage of the cascade and a control of the FNR in each round so as to avoid an exponential increment of the false positives.

• *RUSBoost-based Cascade* (hereafter abbreviated as *RUS*). This approach 308 is based on the random undersampling of the majority class. To this end, 309 we implemented in each node of the cascade the RUSBoost classifier [18]. 310 The training data in input at each stage are undersampled so as to obtain a ratio of 35 : 65 (positive:negative). 312

For the sake of comparison, we have also considered the original Viola-Jones 313 cascade detector (hereafter abbreviated as Ada), where the node stage is built 314 with an AdaBoost dichotomizer. 315

The detectors have been evaluated in terms of Receiver Operating Charac-316 teristics (ROC) curve by plotting True Positive Rate (TPR) against FPR for 317 a series of thresholds on the confidence degree associated to each sample. In 318 this case not all the ROC curve is of interest since only low values of FPR are 319 acceptable. For this reason, our analysis was focused on the initial portion of 320 the curve and, subsequently, we considered as performance measure the *partial* 321 Area Under the ROC Curve (pAUC) defined as $pAUC(x) = \int_0^x TPR \ dFPR$ 322 where [0, x] is the range of interest for FPR [30]. 323

To determine if *RankingCascade* performs significantly different from the 324 other approaches we applied the bootstrap procedure [17]. The test set was 325 sampled with replacement 2,000 times so that each new set of sampled data 326 contained the same number of examples as the original set. We considered 327 two different FPR ranges $[0, 10^{-3}]$ and $[0, 10^{-4}]$ which are close to practical 328 application requirements for all the problems considered. For each range, the 329

Table 1: Performance differences between the compared detectors for a pAUC evaluated at 10^{-3} on the face detection problem.

Methods	Mean Differences	p-value
Ada	$2.19 \cdot 10^{-5}$	< 0.001
Asym	$-4.68 \cdot 10^{-6}$	0.842
$Asym^*$	$6.42 \cdot 10^{-7}$	0.430
RUS	$2.05 \cdot 10^{-5}$	< 0.001

Table 2: Performance differences between the compared detectors for a pAUC evaluated at 10^{-4} on the face detection problem.

Methods	Mean Differences	p-value
Ada	$6.33 \cdot 10^{-6}$	< 0.001
Asym	$3.29 \cdot 10^{-6}$	0.001
$Asym^*$	$1.07 \cdot 10^{-6}$	0.081
RUS	$1.98 \cdot 10^{-5}$	< 0.001

differences in pAUC between RankingCascade and the other detectors were 330 computed. Resampling 2,000 times resulted in 2,000 values for each performance 331 difference. To compare the performance of our approach against the other 4 332 methods we evaluated the *p*-value, defined as the fraction of the corresponding 333 pAUC differences that were negative or zero. The statistical significance level 334 was $\alpha = 0.01$ but, due to the number of comparisons, we applied the Bonferroni 335 correction [6] and thus, performance differences were considered significant if 336 p < 0.0025, (i.e., $p < \alpha/4$). 337

338 5.1. Face Detection

Face detection is the first analyzed problem. Following a common procedure 339 in the literature [22, 23, 28], two different data sets have been created to train 340 and test the cascades. The positives samples for the training phase were 1,600 341 subwindows extracted from the frontal faces of the well-known FERET database 342 [14] and scaled in a standard format of 24×24 pixels. The negative samples 343 were 22,906,769 subwindows, all of size 24×24 , taken from the 9,028 images 344 of a publicly available non-face dataset [28] at different scales. The positive 345 samples were equally parted between training and validation set. The negative 346 samples were divided in three data sets: training set, validation set and pool 347 respectively of 20,000, 60,000 and 22,826,769 samples. As test set we adopted 348

the MIT+CMU database [20, 16] that consists of 180 images containing 734 faces. The negative set has been taken from 1,417 images randomly extracted from different categories (abbey, forests, greenhouse, shipyard, skyscraper) of the publicly available SUN database [29] for a total of 21,181,195 samples.

The cascade detectors were built using d = 0.999 and f = 0.300. The training stage produced 4 nodes for all the cascades except $Asym^*$ that was composed by 6 stages. The total number of features considered at each stage was 116,544.

Results of the comparisons between detectors are reported in Tables 1 and 357 2 for the two FPRs considered in the pAUC evaluation. In both tables, the 358 second column shows the mean difference between the pAUC of the proposed 359 approach and the compared detectors while for each comparison the *p*-value is 360 given in the third column. Statistically significant differences are listed in **bold**. 361 In Table 1 the performance of the proposed method is compared to the 362 other cascades for an FPR lower than 10^{-3} . RankingCascade reveals to be 363 significantly better than Ada and RUS. The differences, instead, are not statis-364 tically significant when compared to $Asym^*$ and Asym. When looking at Table 365 2, i.e., for a pAUC evaluated between 0 and 10^{-4} , results are even better since 366 the performance of our method becomes statistically higher than those of Asym. 367 The difference with $Asym^*$, instead, is again not statistically significant. As a 368 final remark, it is worth noting that Asym is a parametric approach whereas 369 Asym^{*}, using a dynamic optimization of the FPR in each stage, tends to a 370 classification system with a higher number of stages and a higher number of 371 features per stage, so increasing the computational complexity of the cascade. 372

373 5.2. Microcalcification Detection

The second experiment deals with the problem of detecting microcalcifications on digital mammograms. Microcalcifications appear as bright small circular spots in the image and represent a subtle sign of breast cancer in women. A private full-field digital mammographic database of 198 images has been exploited to extract 8,000 microcalcifications (positive samples) and 22,760,320

Table 3: Performance differences between the compared detectors for a pAUC evaluated at 10^{-3} on the microcalcifications detection problem.

Methods	Mean Differences	p-value
Ada	$2.82 \cdot 10^{-5}$	< 0.001
Asym	$8.81 \cdot 10^{-6}$	< 0.001
$Asym^*$	$2.74 \cdot 10^{-5}$	< 0.001
RUS	$9.52 \cdot 10^{-5}$	< 0.001

Table 4: Performance differences between the compared detectors for a pAUC evaluated at 10^{-4} on the microcalcifications detection problem.

Methods	Mean Differences	p-value
Ada	$5.61 \cdot 10^{-6}$	< 0.001
Asym	$3.51 \cdot 10^{-6}$	< 0.001
$Asym^*$	$4.64 \cdot 10^{-6}$	< 0.001
RUS	$1.69 \cdot 10^{-5}$	< 0.001

³⁷⁹ background regions (negative class), all of size 12×12 . Ten-fold cross vali-³⁸⁰ dation has been performed considering 9 folds for training set, validation set ³⁸¹ and pool and the remaining fold as test set. In each cross validation step we ³⁸² used 7,200 positive samples equally parted between training and validation sets ³⁸³ and 20,484,351 negative samples subdivided in 20,000, 60,000 and 20,404,351 ³⁸⁴ respectively for training set, validation set and pool.

The cascade detectors were built using d = 0.99 and f = 0.30. The training stage consists in ten different cross validation runs and thus, for each method, ten different cascades were obtained. The number of stages for the *RankingCascade* was equal to 5 for all the runs while for the other approaches varied among 4 and 6 according to the cross validation step considered. The total number of features considered at each stage was 14,709.

The results of the comparisons for the two different FPRs used in pAUC evaluation (i.e., 10^{-3} and 10^{-4}) are reported respectively in Tables 3 and 4. In both cases the *RankingCascade* exhibits higher performance than all the other approaches even with a high statistical significance as proved by the very low *p*-values.

The effectiveness of the approach on this particular problem has been also confirmed by the results obtained in [1], where it has been employed in a

Table 5: Performance differences between the compared detectors for a pAUC evaluated at 10^{-3} on the microaneurysm detection problem.

Met	thods	Mean Differences	p-value
Ada		$2.82 \cdot 10^{-5}$	< 0.001
Asy	m	$8.81 \cdot 10^{-6}$	< 0.001
Asy	m^*	$2.74 \cdot 10^{-5}$	< 0.001
RUS	5	$9.52 \cdot 10^{-5}$	< 0.001

Table 6: Performance differences between the compared detectors for a pAUC evaluated at 10^{-4} on the microaneurysm detection problem.

Methods	Mean Differences	p-value
Ada	$5.61 \cdot 10^{-6}$	< 0.001
Asym	$3.51 \cdot 10^{-6}$	< 0.001
$Asym^*$	$4.64 \cdot 10^{-6}$	< 0.001
RUS	$1.69 \cdot 10^{-5}$	< 0.001

³⁹⁸ Computer-Aided Detection and Diagnosis (CAD) system that revealed to be ³⁹⁹ competitive with the state-of-the-art commercial CAD systems.

400 5.3. Microaneurysm Detection

The third experiment deals with the problem of detecting microaneurysms 401 on digital ocular fundus images. Microaneurysms appear as a dark small cir-402 cular spots in the image and represent a subtle sign of retinopathy. A pub-403 lic database [15] of 50 digital ocular fundus images has been used to extract 404 2,890,972 patches of size 15×15 pixels, 1,997 containing microaneurysms (pos-405 itive samples) and 2,888,975 containing background tissue (negative samples). 406 Ten-fold cross validation has been performed considering 9 folds for training 407 set, validation set and pool and the remaining fold as test set. In each cross 408 validation step we used 1,797 positive samples equally parted between training 409 and validation sets and 2,620,077 negative samples subdivided in 10,000, 10,000 410 and 2,600,077 respectively for training set, validation set and pool. 411

The cascade detectors were built using d = 0.95 and f = 0.30. The training stage consists in ten different cross validation runs and thus, for each method, ten different cascades were obtained. The number of stages for all the methods considered varied among 14 and 16 according to the cross validation step considered, except for *RUSBoost* where it varied among 3 and 5. The total number

Table 7: Average execution time (in seconds) for selecting a weak learner			
	Face Detection	MC Detection	MA Detection
RankingCascade	22.6	3.5	3.7
Ada	104.7	9.1	12.4
Asym	89.6	11.6	15.8
$Asym^*$	92.2	10.6	15.4
RUS	19.1	3.1	3.3

Table 8: Average execution time (in seconds) for building a node classifier				
	Face Detection	MC Detection	MA Detection	
RankingCascade	360.0	49.4	103.0	
Ada	830.7	107.0	306.2	
Asym	1030.1	135.9	400.3	
$Asym^*$	1625.6	150.9	509.2	
RUS	248.4	34.1	67.5	

417 of features considered at each stage was 43,172.

The results of the comparisons for the two different FPRs used in pAUC evaluation (i.e., 10^{-3} and 10^{-4}) are reported respectively in Tables 5 and 6. In both cases the *RankingCascade* exhibits higher performance than all the other approaches even with a high statistical significance as proved by the very low *p*-values.

423 5.4. Computational time

To confirm the effectiveness of the implementation proposed in Section 4, for 424 each performed experiment we report in Table 7 the average execution time for 425 selecting a weak learner and in Table 8 the average execution time for building 426 a node classifier. All the considered methods have been implemented in C++ 427 with multi-threading and run on a workstation equipped with two Intel Xeon 428 E5520 and 96.0 GB of RAM. Remarkably, RankingCascade performed faster 429 than all the other learning strategies except RUS, which takes advantage of 430 undersampling to drastically reduce the number of calculations (at the cost of 431 worse detection performance, as shown before). 432

433 6. Conclusions

In this paper we have addressed the problem of class imbalance in the node 434 classifier learning within the standard Viola-Jones cascade framework and pro-435 posed a new learning strategy aimed at maximizing the node classifiers ranking 436 capability rather than their accuracy. Such approach revealed to be an effective 437 solution to the class asymmetry problem and provided good performance in ex-438 periments when compared with other approaches. In particular, when tested on 439 three real-world severe detection problems, our learning strategy provided simi-440 lar or better results than methods, such as AsymBoost and AsymBoost*, which 441 rely on a cost-based approach to face class imbalance. In this regard, it is worth 442 mentioning that our method (as well as $AsymBoost^*$) does not introduce any 443 further parameter to the original cascade whereas AsymBoost requires a cost 444 ratio to be specified. In the same experiments, the proposed approach showed 445 significantly better results also when compared with a cascade using RUSBoost, 446 so demonstrating that the ranking-based strategy in node classifier learning 447 performs better than undersampling. In summary, the experimental results 448 supported the rationale on which our method is based, i.e., that ranking-based 449 learning is effective in facing class imbalance and allows the construction of pro-450 ficient cascade detectors. Possible directions for future work include evaluating 451 the effectiveness of the proposed approach also in other cascade architectures 452 which extend the standard Viola-Jones framework. 453

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